Investigation Of Gas-Solid Fluidized Bed With Non-Spherical Particles

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INVESTIGATION OF GAS-SOLID FLUIDIZED BED WITH NON-SPHERICAL PARTICLES

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To my family
INVESTIGATION OF GAS-SOLID FLUIDIZED BED WITH NON-SPHERICAL PARTICLES

by

MARIO A. RUVALCABA, M.S.M.E.

DISSERTATION

Presented to the Faculty of the Graduate School of
The University of Texas at El Paso
in Partial Fulfillment
of the Requirements
for the Degree of

DOCTOR OF PHILOSOPHY

Environmental Science and Engineering Doctoral Program
THE UNIVERSITY OF TEXAS AT EL PASO
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Thanks to all my wonderful friends at UTEP for being there for me at all times. Also, my sincere thanks to all my teachers who have been part of my academic career.

Finally, my acknowledgments would be incomplete if I did not include my family. With the no exception any of them even know exactly what it is I do, but I could never have done it without them. My parents have encouraged me since childhood and always given me a reason to do my best. All of my accomplishments are enabled by the support of my family.
Abstract

The number of experimental and numerical studies of multiphase flows has remarkably increased over the last several years. This research has abundant applications in energy, chemical, and conversion processes. Common use of these technologies includes catalytic cracking for petroleum refineries, fluidized bed reactors (type of chemical reactor), interface modification, and has been an important technology breakthrough in coal gasification. The present work will concentrate on the investigation and validation of gas-solid flows utilizing numerical methods. The gas-solid flows study on this research assumes the solid and gas phases as continua with averaged properties.

The fluid flow computation was achieved using two different solvers: 1) FLUENT a general-purpose CFD code based on the finite volume method on a collocated grid. FLUENT technology offers a wide array of physical models that can be applied to a wide array of industries, 2) MFIX (Multiphase Flow with Interphase eXchanges) a solver developed at the Department of Energy’s National Energy Technology Laboratory (NETL) for multiphase flows. MFIX is a general-purpose hydrodynamic model that describes chemical reactions and heat transfer in dense or dilute fluid-solids flows, typical in energy conversion and chemical processing reactors. MFIX calculations give detailed information on pressure, temperature, composition, and velocity distributions.
# Table of Contents

Acknowledgements............................................................................................................................. v

Abstract........................................................................................................................................ vi

Table of Contents............................................................................................................................... vii

List of Tables ................................................................................................................................... ix

List of Figures ................................................................................................................................... x

Chapter 1: Introduction ..................................................................................................................... 1
  1.1 An Overview on Gas-Solid Flows............................................................................................. 1
  1.2 Understanding the Behavior of Multiphase Flow Fluidized Beds......................................... 2
  1.3 Fluidization of Particles........................................................................................................ 4
  1.4 Approach to Model Gas-Solid Flows.................................................................................... 7
  1.5 Gas-Solid Flows with Non-Spherical Particles................................................................. 7

Chapter 2: Literature Review .......................................................................................................... 9
  2.1 Eulerian-Eulerian Models....................................................................................................... 9
  2.2 Eulerian-Lagrangian Models............................................................................................... 9
  2.3 Non-Spherical Particles Research...................................................................................... 10
  2.4 Overview of Current Work.................................................................................................. 13
  2.5 Practical Relevance............................................................................................................ 13
    2.5.1 Gasification Processes.................................................................................................. 14

Chapter 3: Objectives ..................................................................................................................... 17

Chapter 4: Fluidization .................................................................................................................... 18
  4.1 Fluidized Bed Behavior........................................................................................................ 18
  4.2 Bed Pressure Drop............................................................................................................... 19
  4.3 Flow Modeling..................................................................................................................... 19
  4.4 Theoretical Determination of Minimum Fluidization Velocity........................................ 23

Chapter 5: Simulation Phase Models ............................................................................................... 26
  5.1 Gas-Phase Governing Equations......................................................................................... 26
    5.1.1 Volume Fraction Equation......................................................................................... 26
    5.1.2 Continuity Equation.................................................................................................... 26
List of Tables

Table 1: Geldart’s Classification of Particles
Table 2: Basic Form of Correlations for $Re_{mf}$ Derived from Pressure Drop Principles
Table 3: Borosilicate glass physical properties
Table 4: MFIX simulation parameters
Table 5: Numerical, theoretical and experimental results for spherical particles
Table 6: Non-spherical numerical, theoretical and experimental results
Table 7: Numerical and experimental results comparison
Table 8: Non-spherical numerical, theoretical and experimental results
Table 9: User Defined Function for Syamlal-Obrien with Holzer and Sommerfeld Drag Correlation
Table 10: User Defined Function for Syamlal-Obrien Corrected with Experimentally Developed Drag Correlation
Table 11: MFIX DAT File Example
Table 12: Experimental Drag Coefficient and Reynolds Number Data
List of Figures

Figure 1.1: Fluidized Bed Schematic..........................................................4
Figure 1.2: Geldart Classification of Powders........................................5
Figure 2.1: Fluidized Bed Gasifier...........................................................15
Figure 2.2: Entrained Flow Gasifier.........................................................16
Figure 4.1: Bed Performance with Respect to the Gas Velocity.............18
Figure 6.1: a) Particle Bed Setup b) MFIAX analysis sections.................33
Figure 6.2: Actual photograph showing sphericity analysis of a non-spherical particle........36
Figure 6.3: Non-spherical geometric approximation: a) particle used, b) ellipsoid....38
Figure 6.4: Grid domain and boundary conditions..................................40
Figure 6.5: Grid with particle rectangular-constant-size quad elements region.......41
Figure 6.6: Grid with particle elliptical-constant-size quad elements region........41
Figure 7.1: Fluidized bed experimental setup.........................................45
Figure 7.2: a) High-speed particle motion b) Magnified photographs of spherical particles, and
non-spherical particles.................................................................46
Figure 7.3: Experimental setup.............................................................48
Figure 7.4: Particle motion captured with high-speed camera..................48
Figure 8.1: FLUENT spherical particles validation with experimental results....50
Figure 8.2: MFIAX spherical particles validation with experimental results.....51
Figure 8.3: Snapshots of gas-axial velocity at 75 cm/s inflow velocity with spherical particles...53
Figure 8.4: Snapshots of solids velocity vector-field for inflow velocity of 75 cm/s with spherical Particles.................................................................53
Figure 8.5: Snapshots of solid-phase vol. fraction for inflow velocity of 75 cm/s with spherical particles.................................................................54
Figure 8.6: Comparison of snapshots of bubbling behavior of spherical particles among
simulation (top row) and experiment (bottom row) at t= 2, 5, 7 s from left to right........55
Figure 8.7: Non-spherical particles fluidization curves from simulations results, theoretical
approximation and experimental predictions..........................................56
Figure 8.8: Snapshots of gas-axial velocity at 75 cm/s inflow velocity with non-spherical particles......58
Figure 8.9: Snapshots of solids velocity vector-field for inflow velocity of 75 cm/s with
non-spherical particles.....................................................................58
Figure 8.10: Snapshots of solid-phase vol. fraction for inflow velocity of 75 cm/s with
non-spherical particles.....................................................................59
Figure 8.11: Particle velocity results........................................................60
Figure 8.12: Velocity contours at different times......................................61
Figure 8.13: Fluid force acting on the particle........................................61
Figure 8.14: Drag coefficient vs. Reynolds number of non-spherical particles with sphericity
of 0.55 (105 data points) and its corresponding numerical correlation.............63
Figure 8.15: Non-spherical particles fluidization curves from simulations results, theoretical
approximation and experimental predictions..........................................65
Figure 8.16: Snapshots of gas-axial velocity at 75 cm/s inflow velocity with non-spherical particles......67
Figure 8.17: Snapshots of solids velocity vector-field for inflow velocity of 75 cm/s
with non-spherical particles..............................................................68
Figure 8.18: Snapshots of solid-phase vol. fraction for inflow velocity of 75 cm/s with
non-spherical particles.....................................................................69
Chapter 1: Introduction

1.1 An Overview on Gas-Solid Flows

Theoretical, experimental and numerical studies are being carried out by a variety of research groups to comprehend the gas-solid flow dynamics. Bouillard et al. (1989) used a two fluid model to investigate a fluidized bed with any solid blockages inside the bed. Dasgupta et al. (1997) have developed model for gas-particle flow in a vertical channel. For the solid stress tensor they used the Newtonian model. In such flows, when the particle number increases, the inertial and viscous effects are dominated by the inter-particle collisions. Also a good work in this area may be found in Crowe et al. (1998). Glasser et al. (1998) have performed theoretical studies and computed the solutions for one-dimensional and two-dimensional traveling wave solutions for the equations of motion for gas and particles in a fluidized bed. Glasser et al. used the Newtonian model for the solid stress tensor. Glasser et al. found that the solutions for fully developed two dimensional waves capture the bubble phenomenon in fluidized beds. In fluidized beds regions of high and low particle concentrations are seen to form sporadically. The regions of low particle concentration are known as bubbles and those of high particle concentration are called clusters (Glasser et al., 1998).

Moreover, Detamore et al. (2001) have completed an analysis of scale-up of circulating fluidized beds using kinetic theory. In addition, the modeling of gas-solid flows with combined kinetic theory for the granular phase with continuum representations for the gas phase (Detamore, 2001).
1.2 Understanding the Behavior of Multiphase Flow Fluidized Beds

During the last few decades Computational Fluid Dynamics (CFD) has become a very powerful and versatile tool for the numerical analysis of transport phenomena. With continuously increasing computer power combined with the development of improved physical models CFD has become a very useful tool for chemical engineers. CFD modeling of gas-fluidized beds has proven to be successful and new developments in this area are promising. The majority of studies on modeling of fluidized beds are concerned with the hydrodynamics only. Although attempts have been reported where the hydrodynamics were modeled combined with mass transfer and chemical reaction (Samuelsen and Hjertager, 1996, Gao et al., 1999) the results of such attempts depend strongly on how well the hydrodynamics are modeled. Kuipers and Swaaij (1998) demonstrated that the predicted performance of a riser reactor in terms of chemical conversion depends strongly on the prevailing flow structure in the riser. The authors showed that if the flow structure is not well captured by the hydrodynamic model a sensible prediction of the reactor performance is impossible. Therefore the development of reliable hydrodynamic models is of utmost importance in order to arrive ultimately at models that are capable of predicting the performance of fluidized beds reactors. Hence, the focus of the present study is on the hydrodynamics of the flow.

Multiphase flows can be classified into four categories: gas-liquid, liquid-solid, gas-solid and three phase flows. In this work gas-solid flow type is investigated. A typical example of a gas-solid flow application is a fluidized bed. Conceptually, this device consists of a vertical vessel containing a bed of particles that may range in size from microns to centimeters. A fluid (frequently a gas) is pumped through the porous bottom of the vessel, and through the bed (Wu, 1997). As the gas velocity is increased, initially increasing pressures drop is observed across the bed. Nevertheless, when the pressure drop reaches a value close to the weight of the bed per unit area, the particles become suspended in the
fluid stream and the bed is said to be fluidized. Numerous flow regimes are normally used to explain the characteristics of the flow through a particle bed, these include:

- **Slugging bed**: Bubbles of gas occupy entire fragments of the bed containment vessel and layers are created, splitting the bed into sections.
- **Boiling bed**: A bed in which the gas bubbles are about the same size as the solid particles.
- **Channeling bed**: A bed in which gas channels are formed where most of the gas flows through.
- **Spouting bed**: A bed in which a single gas opening is formed in which some particles flow and fall to the outside. (Geldart, 1973)

A typical fluidized bed schematic is shown in Fig. 1.1. In this system, the solid is in the form of particles that are free to move about in the reactor. Fluidized beds provide more efficient contacting between the solid and the fluid and are integral in enabling catalytic cracking to be a practical, industrial-scale process.
1.3 Fluidization of Particles

In 1973, Professor D. Geldart classified powders that have similar properties into four groups and designated them by the letters A, B, C, and D. This collection is called "Geldart Groups. The groups are defined by their locations on a diagram of solid-fluid density difference \((\rho_s - \rho_f)\) and particle size \((d_p)\). Moreover, fluidized bed design methodologies can be customized based upon the particle's Geldart grouping. A mapping of these groups is shown in Figure 1.2 for air fluidized beds (Glasser, 1998).
Group A: “Prior to the initiation of a bubbling bed phase, beds from these particles will expand by a factor of 2 to 3 at incipient fluidization, due to a decreased bulk density. Most powder-catalyzed beds utilize this group”.

Group B: “Bubbling typically forms directly at incipient fluidization”.

Group C: “This group contains extremely fine and subsequently the most cohesive particles. These particles fluidize under very difficult to achieve conditions, and may require the application of an external force, such as mechanical agitation”.

Group D: “Fluidization of this group requires very high fluid energies and is typically associated with high levels of abrasion. Roasting coffee beans, gasifying coals, and some roasting metal ores are such solids, and they are usually processed in shallow beds or in the spouting mode” (Geldart, 1973).

Detailed characteristics of powders that belong to the four groups are presented in Table 1.
Table 1: Geldart’s Classification of Particles (Gupta and Sathiyamoorthy, 1999).

<table>
<thead>
<tr>
<th></th>
<th>A</th>
<th>B</th>
</tr>
</thead>
<tbody>
<tr>
<td>Example</td>
<td>Cracking catalyst</td>
<td>Sand</td>
</tr>
<tr>
<td>Particle size ($d_p$), $\mu m$</td>
<td>30–100</td>
<td>40 &lt; $d_p$ &lt; 500</td>
</tr>
<tr>
<td>Density ($\rho_s$), kg/m³</td>
<td>&lt;1400</td>
<td>1400 ≤ $\rho_s$ ≤ 4000</td>
</tr>
<tr>
<td>Expansion</td>
<td>Large even before bubbling</td>
<td>Small</td>
</tr>
<tr>
<td>Bed collapse rate</td>
<td>Slow (e.g., 0.3–0.6 cm/s)</td>
<td>Very fast</td>
</tr>
<tr>
<td>Mixing</td>
<td>Rapid even with a few bubbles</td>
<td>Little in the absence of bubbles</td>
</tr>
<tr>
<td>Bubblies</td>
<td>Appear even before $U_{mf}$ (i.e., $U_{re}/U_{mf} &gt; 1$)</td>
<td>Appear after $U_{mf}$ ($U_{re}/U_{mf} \leq 1$)</td>
</tr>
<tr>
<td></td>
<td>Split and recoalesce frequently</td>
<td>Coalescence is predominant</td>
</tr>
<tr>
<td></td>
<td>Rise velocity &gt; interstitial gas velocity</td>
<td>Rise velocity &gt; interstitial gas velocity</td>
</tr>
<tr>
<td></td>
<td>For freely bubbling bed, rise velocity (30–40 cm/s) of small bubble (&lt;4 cm) not dependent on bubble size</td>
<td>Size increases linearly with bed height and excess gas velocity</td>
</tr>
<tr>
<td></td>
<td>Maximum bubble size exists</td>
<td>No evidence</td>
</tr>
<tr>
<td></td>
<td>Cloud-to-bubble-volume ratio is negligible</td>
<td>Cloud-to-bubble-volume ratio not negligible</td>
</tr>
<tr>
<td>Slugs</td>
<td>Slugs produced at high superficial velocity and break</td>
<td>Slugs at high velocity of gas, rise along wall and no evidence of breakdown</td>
</tr>
<tr>
<td></td>
<td>Slug size decreases with $d_p$</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th></th>
<th>C</th>
<th>D</th>
</tr>
</thead>
<tbody>
<tr>
<td>Example</td>
<td>Finer</td>
<td>Coarse</td>
</tr>
<tr>
<td>Particle size ($d_p$), $\mu m$</td>
<td>&lt;60 $\mu m$, if ($\rho_s - \rho_g$) &lt; 500 kg/m³</td>
<td>&gt;500</td>
</tr>
<tr>
<td>Density ($\rho_s$), kg/m³</td>
<td>&lt;1400</td>
<td>&gt;1400</td>
</tr>
<tr>
<td>Expansion</td>
<td>Powder cohesive in nature; difficult to fluidize</td>
<td>Solid particles are spoutable; hence expansion is similar to spouted bed</td>
</tr>
<tr>
<td>Bed collapse rate</td>
<td>Very poor as deaeration is not fast</td>
<td>Fastest of all groups because of dense or large size of particles</td>
</tr>
<tr>
<td>Mixing</td>
<td>Particle mixing as well as heat transfer between a surface and bed are poorer than Group A and B</td>
<td>Solid mixing is relatively poor; high particle momentum and little particle contact minimize agglomeration; gas velocity in dense phase is high, and hence backmixing of dense-phase gas is less</td>
</tr>
<tr>
<td>Bubbling/ fluidization</td>
<td>As the interparticle forces are greater than the force exerted by fluid, the powder lifts as slug in small-diameter column or channel; hence bubbling is absent or not reported</td>
<td>Bubbles form at 5 cm above the distributor</td>
</tr>
<tr>
<td></td>
<td>Agglomeration due to excessive electrostatic force</td>
<td>Bubbles of similar size to those of Group B are possible at same bed height and excess gas flow rate; largest bubbles rise slower than interstitial gas, and hence gas enters the bubble base and comes out at the top</td>
</tr>
<tr>
<td></td>
<td>Fluidization is generally possible by using agitator or vibrator to break the channels</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Electrostatic charges removed by using conductive solids or solids with graphite coating or column wall with oxide coating</td>
<td></td>
</tr>
</tbody>
</table>
1.4 **Approach to Model Gas-Solid Flows**

Generally two different approaches may be taken to model the gas-solid flows:

*Continuum Approach:* This approach is also known as Eulerian-Eulerian approach. The gas and the solid are treated as interpenetrating continua. Here the continuity and momentum equations are written for each phase. This approach requires a constitutive equation for the solid phase to relate the solids stress tensor to the velocity field; the fluid phase is typically modeled as Newtonian. The interphase interaction terms often involve empirical relationships for drag, heat transfer and other exchanges (Jakobsen, 2008).

*Combined Continuum:* Also known as molecular dynamics or Discrete Element Model (DEM). Here the fluid phase is treated as before a Eulerian approach. The solid phase follows the motion of individual particles tracked using Newton’s laws, accounting for collision dynamics between particles. This model includes wall forces and the solid-fluid interaction forces. This approach is known as the Lagrangian approach. Other effects such as heat and mass transfer are also taken into consideration with this Eulerian-Lagrangian approach (Li, 2006).

The focus of this work is the comparison of simulations involving gas-solid flows in a fluidized bed the Continuum approach.

1.5 **Gas-Solid Flows with Non-spherical Particles**

He Tao and Wenqi (2010) developed a DEM method to simulate the corn-shaped particles flow in a hopper. The corn-shaped particle was described by four overlapping spheres. Contact force and gravity force were considered when establishing the model. In addition, the velocity distribution and voidage variance of corn-shaped and spherical particles were investigated. The results showed that the vertical velocity difference between center and side wall and the horizontal velocity of corn-shaped particles were relatively larger than that of spherical particles (He Tao and Wenqi, 2010). Moreover,
Hilton et al. (2009) presented a re-formulation of the pressure-gradient force model, based on a modified pressure correction method, coupled to a discrete element model with non-spherical grains. The drag relations for the coupling were modified to take into account the grain shape and cross-sectional area relative to the local gas flow. They showed that grain shape has a significant effect on the dynamics of the fluidized bed, including increased pressure gradients within the bed and lower fluidization velocities when compared to beds of spherical particles. A model was presented to explain these effects, showing that they are due to both decreased porosity within the bed as well as the relative particle cross-sectional area creating a greater net drag over the bed (Hilton et al., 2009).

For the proposed work, a fundamental goal will be to obtain non-spherical drag models based on numerical work, the drag force will be assumed as a function of several experimental parameters ($C_D$, $Re$, $Q$, $g$, etc.). Implementation of this relationship will be done in MFIX. In conjunction with the derived correlations drag relationships will also be compared to those shown by Hilton et al. (2009) where prediction of $C_D$ was estimated as a function of sphericity, as shown in Eqn. (1.1). The sphericity ($\Phi$) represents the ratio between the surface area of the volume equivalent sphere and that of the considered particle, the cross-wise sphericity ($\Phi_\perp$) is the ratio between the cross-sectional area of the volume equivalent sphere and the projected cross-sectional area of the considered particle and the lengthwise sphericity ($\Phi_{||}$) is the ratio between the cross-sectional area of the volume equivalent sphere and the difference between half the surface area and the mean projected longitudinal cross-sectional area of the considered particle. Finally, the numerical modeling of particulate and fluid flows will be compared to experimental results obtained for non-spherical particles.

$$C_D = \frac{8}{Re} \frac{1}{\sqrt{\Phi_{||}}} + \frac{16}{Re} \frac{1}{\sqrt{\Phi}} + \frac{3}{\sqrt{Re \Phi^3}} + 0.42 10^{0.4(-\log \Phi)^{0.2}} \frac{1}{\Phi_{\perp}}$$

(1.1)
Chapter 2: Literature Review

2.1 Eulerian-Eulerian Models

In general, the Eulerian-Eulerian approach is computationally more efficient and therefore can be applied to systems with a larger number of particles than the Eulerian-Lagrangian approach, which is limited to approximately 100,000 particles. However, incorporation of complex particle physics (e.g., cohesion) is a more difficult task with Eulerian-Eulerian models. The impact of cohesion on such a continuum quantity is more difficult to model than its incorporation on a particle-particle level (as is necessary for the Eulerian-Lagrangian approach). The focus of many subsequent Eulerian-Eulerian efforts has been to incorporate improved constitutive relations for the solid phase. A detailed review of these advances for kinetic-theory relations is given in reviews by Campbell (1990) and Goldhirsch (2003). For a thorough review of the associated Eulerian-Eulerian models, the reader is referred to Enwald et al. (1996), Sinclair (1997) and Van Wachem and Almstedt (2003).

2.2 Eulerian-Lagrangian Models

One of the first efforts to develop an Eulerian-Lagrangian fluidized bed simulation was made by Tsuji et al. (1993). This effort used a soft-sphere, discrete particle treatment, similar to what had been developed by Cundall and Strack (1979) combined it with an Eulerian model for the gas flow. This simulation was used to study bubble flow and the results were shown to compare reasonably well with laboratory experiments. Subsequently the soft-sphere method has been used to study a wide variety of systems. Some examples of topics that have been studied using the soft-sphere method include bubble formation (Gera et al., 1998), mixing (Rhodes et al., 2001), binary systems (Limtrakul et al., 2003), and cohesive systems (Mikami et al., 1998, Rhodes and Wang, 2000, Rhodes et al., 2001, Rhodes et al., 2001). A noted drawback of the soft-sphere approach is that the particles are often made artificially soft.
in order to keep the simulation stable (Xu and Yu, 1997). Nonetheless, many efforts have shown that the artificially soft nature of particles in soft-sphere models does not affect the overall particle flow (Gera et al., 1998, Mikami et al., 1998, Kawaguchi et al., 1998, Renzo and Maio, 2004).

Studies by Xu and Yu (1997) and Xu et al. (2000) developed a model that utilized a time-stepped algorithm, however, for each particle overlap the simulation was reversed so that the particles “back-up” to point of incipient contact. The repulsive force was still calculated using a soft-sphere model, but the maximum overlap was limited. This “predictor-corrector” method was used to produce realistic fluidized bed snapshots and pressure drop data.

An alternative to the soft-sphere approach is the application of a hard-sphere technique for the simulation of gas-solid systems. This combination was first utilized by Hoomans et al. (1996). In this system, gas-particle interactions are implemented followed by several collisions which are processed one (instantaneous) collision at a time. Some examples of systems that have been studied using this approach include binary systems (Hoomans et al., 2000), bubbling (Ouyang and Li, 1999, Yuu et al., 2000), clustering (Helland et al., 2000, Van Wachem et al., 2001) and high pressure fluidization (Li and Kuipers, 2002), specific applications such as coal combustion (Zhou et al., 2003) and spray granulation (Goldschmidt et al., 2003).

2.3 Non-Spherical Particles Research

In related areas, several researchers have investigated the effect of particle shape on drag. Most of this work consists of the development of formulas to predict the drag coefficient for particles of various shapes in a stationary fluid. Examples include Hartman et al. (1994), Ganser (1993), Haider and Levenspiel (1989), Swamee and Ojha (1991) and Trang-Cong et al. (2003). All of these researchers show a significant influence of particle shape on drag coefficient. The effect of shape on drag and the methods for determining the drag are also given by Clift et al. (1978). Since non-spherical particles have
different drag coefficients, the changes in interaction with the fluid should be significant. Although research has been done on the drag of non-spherical particles, very few experiments have been attempted to document how the particle’s shape affects the flow. An exception to this is research that has been done on free-falling non-spherical particles in the atmosphere (Klett, 1995) where a theoretical investigation was made on predicting the orientation of falling non-spherical particles in the atmosphere and the work of Black (1997), comparing the flow behavior of spherical and non-spherical particles in a confined geometry. In Black’s (1997) research he completed several different projects in conjunction with his dissertation. One of these projects was measuring particle size, velocity, and concentration in both a coaxial jet flow and a swirling flow through a cylindrical chamber using both spherical and non-spherical particles. His results showed a significant difference in the flow characteristics between the spherical versus non-spherical particles. However, since then the results of his measurements for the non-spherical particles have been shown to be questionable since his measurement techniques permitted serious small particle bias. Additionally, while the data generated by Black (1997) involves non-spherical particles, the flow through the cylindrical chamber introduces swirl which is difficult to model numerically and therefore produces too much uncertainty in the fluid modeling to allow an evaluation of the particle modeling. A review of laser-based particle measuring methods has also been previously completed by Black et al. (1995), including the laser-based instrumentation for particle analysis available at BYU. The review of the literature related to the behavior of non-spherical particle flow in a backward-facing step shows that there is a need for measurements to be made in order to develop and validate existing computer models and provide valuable information regarding the flow behavior of non-spherical particles.

Additionally, there is evidence showing that a turbulent fluid can significantly increase the drag coefficient of particle especially for non-spherical particles. While very little literature is available discussing the effects turbulent fluids have on the drag on particles, Brucato et al. (1998) studied the
effects that turbulence had on the settling velocities of particles versus that in a still fluid. In their experiment they were able to measure the average particle drag coefficients in a turbulent media by means of a suitable residence time technique of the settling velocity exhibited by a cloud of particles. The data they obtained confirmed that free stream turbulence can significantly increase or decrease a particle’s drag coefficient when compared with a still fluid without free stream turbulence.

Moreover, Escudie´a et al. (2006) have experimentally investigated shape based segregation in fluidized beds showing particles with the same volume, but different shape, can segregate. Liu and Litster (1991) investigated the effects of non-spherical particles on the properties of spouted beds. Later, Liu et al. (2008) also investigated the effects of particle shape on both pressure drop and minimum fluidization velocity and showed that all of the shapes considered had lower fluidization velocities than for spheres. Combined theoretical and experimental work has been undertaken specifically determining the effects of particle shape on column pressure drop in packed beds (Dolej´s and Machac, 1995).

Existing dynamic fluidized bed models in the literature assume spherical particle geometry; nonetheless, in industry particles are hardly ever spherical. Non-spherical simulations with shapes including ellipsoidal, cubic and super-quadric particles, have been applied in industry. The particle shape effect in granular flow was investigated by Cleary (2008), and Fraige et al. (2008). Mixing was investigated by Cleary et al. (1998), were demonstrated that predicting realistic mixing rates was unable to predict with circular particles. Moreover, Cleary and Metcalfe (2002) predicted mixing rates in the correct order with the inclusion of particle shape. Lastly, the effect of particle shape on many other industrial applications is summarized in Cleary (2004, 2009). Nevertheless, particle shape effect in fluidized beds has become and imperative factor computationally.
2.4 Overview of Current Work

Continuum models treat the particles as a continuous phase via a mass and momentum balance for that phase, along with appropriate constitutive equations. For rapid flows, a kinetic-theory analogy (Campbell, 1990, Goldhirsch, 2003) is typically used to develop constitutive relations needed for continuum models. Inherent in the kinetic-theory approach is the assumption that particle-particle interactions are both binary and instantaneous. As mentioned previously, cohesive forces are not inherently instantaneous and therefore the incorporation of cohesive forces into the kinetic theory framework is not straightforward. Unlike continuum models, discrete-particle simulations track particles in the system via the solution of a separate momentum balance for each particle. Most existing descriptions for particle cohesion can be applied to discrete-particle models while not conflicting with any assumptions inherent in the simulation.

Discrete-particle simulations provide a straightforward means of incorporating interparticle attraction because cohesive forces can be applied directly to each particle-particle interaction. Discrete-particle simulations are limited by the computational requirements arising from the solution of a separate momentum balance for each particle. Continuum models based on the kinetic theory provide a less computationally demanding means of investigating particulate flows but are restricted by the assumptions implicit in their constitutive relations (e.g. instantaneous, binary contacts).

2.5 Practical Relevance

In the last decades, the experimental and numerical studies of multiphase flows have surprisingly increased especially gas-solid flows. Investigation of this type has abundant applications in energy, chemical processes, among others. Likewise, fluidization has an important technology breakthrough in coal gasification.
2.5.1 Gasification processes

Gasification is a process that converts carbonaceous materials, such as coal, petroleum, biofuel, or biomass, into CO and H\(_2\) (syngas) by reacting the raw material at high temperatures with a controlled amount of oxygen and/or steam. For this purpose a fluidized bed is used.

Fluidized bed gasifiers as shown in Fig. 2.1 are most useful for fuels that form highly corrosive ash that would damage the walls of slagging gasifiers. Biomass fuels generally contain high levels of corrosive ash. Fuel throughput is higher than for fixed bed gasifiers, but not as high as for the entrained flow gasifier. In entrained flow gasifiers as shown in Fig. 2.2 a dry pulverized solid, an atomized liquid fuel or fuel slurry is gasified with oxygen in co-current flow. The gasification reactions take place in a dense cloud of very fine particles. The high temperatures and pressures mean that a higher throughput can be achieved; however thermal efficiency is somewhat lower as the gas must be cooled before it can be cleaned with existing technology. The high temperatures also mean that tar and methane are not present in the product gas; however the oxygen requirement is higher than for the other types of gasifiers.
Figure 2.1: Fluidized Bed Gasifier (FAO, 2010)
Figure 2.2: Entrained Flow Gasifier (DOE, 2010)
Chapter 3: Objectives

The specific objectives of the proposed work are to:

1. To apply the coupled gas-solid flow capability to the investigation of the detailed physics of fluidized beds. Of particular interest is the investigation of particle size and shape effects.

2. Study the effect of the various drag correlations (published in literature) on the simulation results.

3. To Incorporate Experimental Data for Non-Spherical Particles in MFIX and Fluent, by numerically modeling the minimum fluidization velocities, drag, particle, and fluid flows of non-spherical particles in the fluidized bed.

4. Validate model based on experimental results.
Chapter 4: Fluidization

4.1 Fluidized Bed Behavior

Once the fluid flow rate is increased to produce incipient fluidization, this flow rate value is quoted as a velocity termed “minimum fluidization velocity”, $U_{mf}$, defined as

$$U_{mf} = \frac{\dot{V}_{mf}}{A} \quad (4.1)$$

Where $\dot{V}_{mf}$ is the volume flow rate at incipient fluidization and $A$ is the cross-sectional area of the bed containment (Howard, 1989).

Figure 4.1 shows how the pressure drop across the bed changes with respect to the gas velocity.

![Bed Performance with Respect to the Gas Velocity](image)

Figure 4.1: Bed Performance with Respect to the Gas Velocity
4.2 Bed Pressure Drop

Once fluidization has been achieved, the pressure drop across the bed, $\Delta P_b$, will be sufficient to support the particle weight, thus

$$\Delta P_b = \frac{M}{\rho_p A} \left( \rho_p - \rho_f \right) g$$

(4.2)

Where $M$ is the mass of the particles, $\rho_p$ is the particle density, $\rho_f$ is the fluid density, $A$ is the cross-sectional area of the bed containment and $g$ is the gravitational constant (Howard, 1989).

If the density of the fluid is negligible compared to the one of the particles, Equation (4.2) can be simplified to

$$\Delta P_b = \frac{M g}{A}$$

(4.3)

4.3 Flow Modeling

The approach used by Ergun and Orning (1949) modeled a packed bed as a series of identical, straight, parallel channels, and then to form an equation of the form, pressure gradient:

$$\frac{dp}{dx} = \alpha v + \beta v^2$$

(4.4)

Where $v$ is the fluid velocity through the channels and $\alpha$ and $\beta$ are coefficients. The first and second terms in equation (4.4) are subsequently multiplied by the dimensionless correlation factors $\alpha$ and $\beta$, respectively (Howard, 1989).

Thus

$$\frac{dp}{dx} = \alpha a v + \beta b v^2$$

(4.5)

Values of $\alpha$ and $\beta$ were determined by conducting experiments. The coefficient $a$ was obtained from the well known Hagen-Poiseuille equation for Pressure Drop, $\Delta P_v$, over the length, $L$, of a single straight tube of circular cross section of diameter $d$, in which the flow is entirely laminar, thus
\[
\frac{\Delta P_v}{L} = \frac{32 \mu_f v}{d^2} \quad (4.6)
\]

where \( v \) is the mean fluid velocity through the tube and \( \mu_f \) is the viscosity.

The pressure drop \( \Delta P_k \) due to dissipation of kinetic energy in eddies or turbulence will be

\[
\frac{\Delta P_k}{L} = \frac{1}{2} \rho_f v^2 \frac{f}{L} \quad (4.7)
\]

Where \( f \) is a dimensionless friction factor, taken in this case as being equal to \( L/d \).

The total pressure drop \( \Delta P_b \) over the length \( L \) is therefore

\[
\frac{\Delta P_b}{L} = 32 \mu_f \frac{v}{d^2} + \frac{1}{2d} \rho_f v^2 \quad (4.8)
\]

If the bed is considered to be composed of \( N \) such tubes in parallel, then their length \( L \) and diameter \( d \) can be expressed in terms of the surface area and volume of solid particles in the bed and the bed voidage.

The surface area of the tube walls:

\[
A_w = N \pi d L \quad (4.9)
\]

And the volume of the fluid in the tubes

\[
V_f = \frac{N \pi d^2 L}{4} \quad (4.10)
\]

Thus

\[
\frac{surface \ area \ of \ tube \ walls}{volume \ of \ fluid \ in \ tubes} \cdot \frac{A_w}{V_f} = \frac{4}{d} \quad (4.11)
\]

If the bed of particles is of depth, containment diameter \( D \) and voidage \( \varepsilon \) then the surface area of particles

\[
= \sum (n_p s_p) \quad (4.12)
\]

Where \( n_p \) and \( s_p \) are the number and surface area of particles of each size, \( p \), in the bed, the volume of solid particles

\[
= \sum (n_p \nu_p) = (1 - \varepsilon) \frac{\pi}{4} D^2 L \quad (4.13)
\]
Where $v_p$ is the volume of each particle of each size and the volume of voids

$$v_p = \varepsilon \frac{\pi D^2 L}{4}$$

Now the surface-to-void volume of the bed, $S_{v \nu}$, is to be the same as that of the cluster of tubes,

$$4 \sum (n_p v_p) (\varepsilon \pi D^2 L)^{-1} = \frac{4}{d}$$

However, from eqn. (4.11)

$$\pi D^2 L = (4 \sum (n_p v_p)) (1 - \varepsilon)^{-1}$$

Inserting this into eqn. (4.13) gives

$$d = \left( \frac{4 \varepsilon}{1 - \varepsilon} \right) \frac{1}{S_v}$$

Now the fluid velocity $v$, through the voids, is related to a superficial fluidizing velocity $U$ by

$$v = \frac{U}{\varepsilon}$$

Substituting for $v$ and $d$ in eqn. (4.8) leads

$$\frac{\Delta P_b}{L} = 2 \frac{(1 - \varepsilon)^2}{\varepsilon^2} \mu_f S_v U^2 + \frac{1}{8} \frac{(1 - \varepsilon)}{\varepsilon^3} \rho_f S_v U^2$$

Inserting the dimensionless correlation factors $\alpha$ and $\beta$ gives

$$\frac{\Delta P_b}{L} = 2 \alpha \frac{(1 - \varepsilon)^2}{\varepsilon^2} \mu_f S_v U^2 + \frac{\beta}{8} \frac{(1 - \varepsilon)}{\varepsilon^3} \rho_f S_v U^2$$

Ergun (1952) took the matter further; pointing out that it is customary to use a particle mean size $d_m$ in pressure drop calculations. For spherical particles

$$d_m = \frac{6}{S_v}$$

Substitution of this into eqn. (4.21) gives

$$\frac{\Delta P_b}{L} = 72 \alpha \frac{(1 - \varepsilon)^2}{\varepsilon^2} \frac{\mu_f U}{d_m^2} + \frac{3 \beta}{4} \frac{(1 - \varepsilon)}{\varepsilon^3} \rho_f \frac{U^2}{d_m}$$
(If particles are non-spherical and are of sphericity \( \varphi \) and mean size \( d \) then \( d_m \) is replaced by the product \( \varphi \cdot d \).)

Dividing each side of the eqn. (3.23) by \((1 - \varepsilon)^2 \mu_f U / \varepsilon^3 d_m^2 \) gives

\[
\frac{\Delta P_b \varepsilon^3 d_m^2}{L \mu_f U (1-\varepsilon)^2} = 72 \alpha + \frac{3 \beta}{4} \frac{1}{(1-\varepsilon)} \frac{\rho_f U d_m}{\mu_f}
\]

(4.24)

Where \( \rho_f U d_m / \mu_f \) is the particle Reynolds Number \( Re_p \).

Ergun plotted a large amount of data from experiments with different types and sizes of particle and different fluids using equation (4.24). The values of 72\( \alpha \) and 3\( \beta / 4 \) were found to be 150 and 1.75 respectively. Therefore equation (4.24) is rearranged in the following fashion also for non-spherical particles of sphericity \( \varphi \):

\[
\frac{\Delta P_b}{L} = 150 \frac{(1-\varepsilon)^2}{\varepsilon^3} \frac{\mu_f U}{(\varphi \cdot d_m)^2} + 1.75 \frac{(1-\varepsilon)}{\varepsilon^3} \frac{\rho_f U^2}{\varphi \cdot d_m}
\]

(4.25)

Eqn. (4.25) is commonly known as the “Ergun equation”. The first term of the equation is linear in \( U \) and this is dominant when the flow in the voids is laminar. The second term is referred to turbulence (Howard, 1989).
4.4 Theoretical Determination of the Minimum Fluidization Velocity

By equating the Pressure drop across a packed bed, given by the Ergun equation to that of a fluidized bed, and solving for the velocity $U$, the obtained value will be the minimum fluidization velocity $U_{mf}$. The previous approach was suggested by Ergun and Orning (1949) (Howard, 1989).

Moreover, substituting $(1 - \varepsilon)(\rho_p - \rho_f)gL$ (where $g$ is the gravitational acceleration) for $\Delta P_b$, $\varepsilon_{mf}$ for $\varepsilon$, and $U_{mf}$ for $U$ in equation (3.25) lead to:

$$
(1 - \varepsilon)(\rho_p - \rho_f)gL = 150 \frac{(1-\varepsilon_{mf})^2}{\varepsilon_{mf}^3} \frac{\mu_f U_{mf}}{(\varphi d_m)^2} + 1.75 \frac{(1-\varepsilon_{mf})}{\varepsilon_{mf}^3} \frac{\rho_f U_{mf}^2}{\varphi d_m}
$$

(4.26)

Multiplying each side by $\rho_f d_m^3 / \mu_f^2 (1 - \varepsilon_{mf})$ gives

$$
\frac{\rho_f (\rho_p - \rho_f) g d_m^3}{\mu_f^2} = 150 \frac{(1-\varepsilon_{mf})}{\varepsilon_{mf}^3} \frac{\rho_f U_{mf} d_m}{(\varphi d_m)^2} + \frac{1.75}{\varepsilon_{mf}^3} \frac{\rho_f^2 U_{mf}^2 d_m^2}{\mu_f^2}
$$

(4.27)

The left-hand side of eqn. (4.27) is the dimensionless number known as the Archimedes Number, $Ar$:

$$
Ar = \frac{\rho_f (\rho_p - \rho_f) g d_m^3}{\mu_f^2}
$$

(4.28)

On the right-hand side of Eqn. (4.27) appears the Reynolds Number based on the minimum fluidization velocity and particle diameter. Thus:

$$
Ar = 150 \frac{(1-\varepsilon_{mf})}{\varepsilon_{mf}^3} Re_{mf} + \frac{1.75}{\varepsilon_{mf}^3} Re_{mf}^2
$$

(4.29)
Furthermore, Wen and Yu were the first to use this type of correlation and to solve it for $Re_{mf}$. In order to arrive at a suitable solution, Wen and Yu collected the data for $\varepsilon_{mf}$ and $\varphi_s$ and the following approximations were found:

$$\frac{(1-\varepsilon_{mf})}{\varphi^2\varepsilon_{mf}^3} \approx 11 \quad \text{and} \quad \frac{1.75}{\varphi\varepsilon_{mf}^3} \approx 14 \quad (4.30)$$

The Wen and Yu correlation expressed using $Re_{mf}$ and $Ar$ is

$$Ar = 24.5Re_{mf}^2 + 1650Re_{mf} \quad (4.31)$$

The solution for $Re_{mf}$, which has the form given in eqn. (4.29), can be written as:

$$Re_{mf} = \left( (A_1 + B_1 Ar) \right)^{1/2} - A \quad (4.32)$$

The values of $A_1$ and $B_1$ depend on the experimental conditions and the range of $Re_{mf}$. The values of constants $A_1$ and $B_1$ in eqn. (4.32) that satisfy the various correlations reported in the literature by various researchers are presented in Table 2 (Gupta and Sathiyamoorthy, 1999).
Table 2: Basic Form of Correlations for $Re_{mf}$ Derived from Pressure Drop Principles (Gupta and Sathiyamoorthy, 1999)

<table>
<thead>
<tr>
<th>Ref.</th>
<th>Constants</th>
<th>Remarks</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$A_i$</td>
<td>$B_i$</td>
</tr>
<tr>
<td>Ergun$^{42}$</td>
<td>42.85/$\alpha$</td>
<td>0.57/$\beta$</td>
</tr>
<tr>
<td>Wen and Yu$^{63}$</td>
<td>33.7</td>
<td>0.0408</td>
</tr>
<tr>
<td>Bourgeois and Grenier$^{44}$</td>
<td>25.46</td>
<td>0.0382</td>
</tr>
<tr>
<td>Ghosal and Mukherjee$^{45}$</td>
<td>29.2</td>
<td>0.029</td>
</tr>
<tr>
<td>Saxena and Vogel$^{46}$</td>
<td>25.28</td>
<td>0.0571</td>
</tr>
<tr>
<td>Babu et al.$^{47}$</td>
<td>25.25</td>
<td>0.0651</td>
</tr>
<tr>
<td>Richardson and Jeromingo$^{48}$</td>
<td>25.7</td>
<td>0.0365</td>
</tr>
<tr>
<td>Thonglimp et al.$^{49}$</td>
<td>19.9</td>
<td>0.03196</td>
</tr>
<tr>
<td>Chitester et al.$^{50}$</td>
<td>20.7</td>
<td>0.0494</td>
</tr>
<tr>
<td>Thonglimp et al.$^{30}$</td>
<td>31.6</td>
<td>0.0925</td>
</tr>
<tr>
<td>Masaaki et al.$^{51}$</td>
<td>33.95</td>
<td>0.0465</td>
</tr>
<tr>
<td>Agarwal and O’Neill$^{52}$</td>
<td>42.81</td>
<td>0.061</td>
</tr>
<tr>
<td>Satyanarayana and Rao$^{53}$</td>
<td>30.10</td>
<td>0.0417</td>
</tr>
<tr>
<td>Grace$^{54}$</td>
<td>27.2</td>
<td>0.0408</td>
</tr>
<tr>
<td>Panigrahi and Murty$^{55}$</td>
<td>32.2</td>
<td>0.0382</td>
</tr>
</tbody>
</table>

Correlation: $Re_{mf} = (A_i + B_i d_2)^{1/2} - A_1$, $\alpha = (1 - \epsilon)d_0^2/\epsilon^2$, $\beta = 1/\epsilon^2$, $m = \alpha/\beta$.
Chapter 5: Simulation Phase Models

5.1 Gas-Phase Governing Equations

5.1.1 Volume Fraction Equation

By means of the averaging approach to model equations, new field variables are introduced. These are the phasic volume fractions; they represent the fraction of averaging the volume taking place by various phases. By concept, the volume fractions of all the phases must add to one:

\[ \varepsilon_g + \varepsilon_s = 1 \]  

(5.1)

where \( \varepsilon_g \) is the volume for the fluid phase, also known as the void fraction, and \( \varepsilon_s \), the volume fraction for the solid phase (Syamlal et al., 1993).

5.1.2 Continuity Equation

The fluid phase is modeled by solving an average mass and momentum balance. The continuity equation is given by:

\[ \frac{\partial}{\partial t} \left( \varepsilon_g \rho_g \right) + \nabla \cdot \left( \varepsilon_g \rho_g \mathbf{v}_g \right) = 0 \]  

(5.2)

where \( \varepsilon_g \) is the void fraction, \( \rho_g \) is the gas density and \( \mathbf{v}_g \) is the gas velocity. The first term in equation (5.2) represents the increase of mass per unit volume and the second term represents the flux of convective mass per unit volume (Anderson and Jackson, 1967).

5.1.3 Momentum Equation

The balance of momentum is given by

\[ \frac{\partial}{\partial t} \left( \varepsilon_g \rho_g \mathbf{v}_g \right) + \nabla \cdot \left( \varepsilon_g \rho_g \mathbf{v}_g \mathbf{v}_g \right) = \nabla \cdot \mathbf{S}_g + \varepsilon_g \rho_g \mathbf{g} - \mathbf{I}_{gs} \]  

(5.3)

where the first term on the left-hand side refers to the increase of momentum per unit volume and the second term refers to the rate of momentum gain by convection per unit volume. On the right-hand side,
the first term describes the rate of momentum transfer by normal and shear stress components per unit volume; $\overline{S_g}$ is the gas-phase stress tensor, the second term explains the net gravitational force on the fluid per unit volume; $\mathbf{g}$ is the acceleration due to gravity, and the last term represents the interaction force between the fluid and solid phases per unit volume; $\overline{I_{gs}}$ is the rate of momentum transfer between the gas and solid phase per unit volume (Syamlal et al., 1993).

The gas-solid momentum transfer is described by:

$$
\overline{I_{gs}} = -\varepsilon_s \nabla P_g - F_{gs}(\overline{v_s} - \overline{v_g})
$$

where $P_g$ is the gas-phase pressure and $\overline{v_s}$ is the average solids velocity. The drag coefficient $F_{gs}$ is determined by two types of experimental data. One type is available as correlations for the terminal velocity. In fluid dynamics an object is moving at its terminal velocity if its speed is constant due to the restraining force exerted by the air, water or other fluid through which it is moving. A free-falling object achieves its terminal velocity when the downward force of gravity (weight) equals the upward force of drag. This causes the net force on the object to be zero, resulting in an acceleration of zero.

5.2 Drag Correlations

5.2.1 Syamlal-Obrien Correlation

Syamlal and O’Brien derived the following equation for converting terminal velocity correlations to drag correlations (Syamlal and O’Brien, 1989):

$$
F_{gs} = \frac{3\varepsilon_s\varepsilon_g P_g}{4v_t^2 d_p} C_{D-sphere} |\overline{v_s} - \overline{v_g}|
$$

(5.5)
where $d_p$ is the particle diameter and $v_t$ is the terminal velocity. The single-sphere drag coefficient $C_{D\text{-sphere}}$ is defined by the formula given by Dalla Valle (Dalla Valle, 1948):

$$C_{D\text{-sphere}} = \left( 0.63 + 4.8 \sqrt{\frac{v_t}{Re}} \right)^2$$  \hspace{1cm} (5.6)

The terminal velocity $v_t$ is described by the following correlation modeled by Garside and Al-Dibouni (Syamlal, 1987):

$$v_t = 0.5 \left( A - 0.06Re + \sqrt{(0.06Re)^2 + 0.12Re(2B - A) + A^2} \right)$$  \hspace{1cm} (5.7)

where

$$A = \varepsilon_g^{4.14}$$  \hspace{1cm} (5.8)

$$B = \begin{cases} 
0.8\varepsilon_g^{1.28} & \varepsilon_g \leq 0.85 \\
\varepsilon_g^{2.65} & \varepsilon_g > 0.85 
\end{cases}$$  \hspace{1cm} (5.9)

and the Reynolds number, $Re$ is defined as

$$Re = \frac{d_p|\bar{v}_s - \bar{v}_g|\rho_g}{\mu_g}$$  \hspace{1cm} (5.10)

where $\mu_g$ is the gas viscosity (Richardson and Zaki, 1954).

### 5.2.2 Gidaspow Correlation

The other type of data available for drag formulation, is valid for high value of solids volume fraction, is packed-bed pressure data expressed in the form of a correlation, such as the Ergun equation. Such a correlation must be complemented with a drag correlation for low values of the solids volume fraction. Such correlation is the Gidaspow drag correlation (Gidaspow et al., 1992):
The single-sphere drag coefficient $C_{D\text{-sphere}}$ is defined by the formula

$$
F_{gs} = \begin{cases} 
\frac{3}{4} C_{D\text{-sphere}} \frac{\rho_s \varepsilon_g \overline{v_s - v_g}}{d_p} \varepsilon_g^{-2.65} & \varepsilon_g \geq 0.8 \\
\frac{150 \varepsilon_s (1-\varepsilon_g) \mu_g}{\varepsilon_g d_p^2} + \frac{1.75 \rho_s \varepsilon_s |\overline{v_s - v_g}|}{d_p} & \varepsilon_g < 0.8
\end{cases}
$$

(5.11)

and the Reynolds number, $Re$ is defined as

$$
Re = \frac{\varepsilon_g \rho_g |\overline{v_s - v_g}| d_p}{\mu_g}
$$

(5.13)

5.3 Solid-Phase Governing Equations

5.3.1 Continuity Equation

The solid phase is modeled by solving an average mass and momentum balance. The continuity equation is given by:

$$
\frac{\partial}{\partial t} (\varepsilon_{sm} \rho_{sm}) + \nabla \cdot (\varepsilon_{sm} \rho_{sm} \overline{v_{sm}}) = 0
$$

(5.14)

where $\varepsilon_{sm}$ is the $m^{th}$ solids volume fraction, $\rho_s$ is the $m^{th}$ solids density and $\overline{v_s}$ is the $m^{th}$ solids velocity.

The first term in equation (5.14) represents the increase of mass per unit volume and the second term represents the flux of convective mass per unit volume (Syamlal, 1987).
5.3.2 Momentum Equation

The balance of momentum is given by

\[
\frac{\partial}{\partial t}(\varepsilon_{sm} \rho_{sm} \bar{v}_{sm}) + \nabla \cdot (\varepsilon_{sm} \rho_{sm} \bar{v}_{sm} \bar{v}_{sm}) = \nabla \cdot \bar{S}_{sm} + \varepsilon_{sm} \rho_{sm} \bar{g} + \bar{I}_{gs} - \bar{I}_{ml} \tag{5.15}
\]

where the first term on the left-hand side refers to the increase of momentum per unit volume and the second term refers to the rate of momentum gain by convection per unit volume. On the right-hand side, the first term describes the rate of momentum transfer by normal and shear stress components per unit volume; \(\bar{S}_{sm}\) is the \(m^{th}\) solids stress tensor, the second term explains the net gravitational force on the solids per unit volume; \(\bar{g}\) is the acceleration due to gravity, the next term represents the interaction force between the fluid and \(m^{th}\) solid phase per unit volume; \(\bar{I}_{gs}\) is the rate of momentum transfer between the gas and solid phase per unit volume, and the last term \(\bar{I}_{ml}\) is the rate of momentum transfer between the different solid phases per unit volume.

The gas-solid momentum transfer is described by:

\[
\bar{I}_{ml} = F_{ml}(\bar{v}_{sl} - \bar{v}_{sm}) \tag{5.16}
\]

where \(\bar{v}_{sl}\) is the average solids velocity for the \(l^{th}\) solid phase, \(\bar{v}_{sm}\) is the average solids velocity for the \(m^{th}\) solid phase The drag coefficient \(F_{sl}\) is represented by a relation derived by Syamlal:

\[
F_{ml} = \frac{3(1+e_{lm})(\pi/2+c_{f-\Delta m}^2/8)\varepsilon_{sl}\rho_{sl}\varepsilon_{sm}\rho_{sm}(d_{pl}^3+d_{pm}^3)^2 g_{o-\Delta m}|\bar{v}_{sl}-\bar{v}_{sm}|}{2\pi(\rho_{sl}+\rho_{sm})^{3/2}} \tag{5.17}
\]
where $e_{tm}$ and $C_r$ are the coefficient of restitution and the coefficient of friction, between the $l^{\text{th}}$ and $m^{\text{th}}$ solid phase particles. The radial distribution function $g_{o-lm}$ is a correction factor that modifies the probability of collisions between grains when the solid granular phase becomes dense. The following equation was derived by Lebowitz for a mixture of hard spheres (Ogawa et al., 1980):

$$g_{o-lm} = \frac{1}{\varepsilon_g} + \frac{3d_{pl}d_{pm}}{\varepsilon_g^2(d_{pl}+d_{pm})} \sum_{n=l}^{M} \frac{\varepsilon_{sn}}{d_{pn}}$$ (5.18)

### 5.4 Modeling Turbulence: The $k$-$\varepsilon$ model

The $k$-$\varepsilon$ model belongs to the class of two-equation models, in which model transport equations are solved for two turbulence quantities—i.e. $k$ and $\varepsilon$ in the $k$-$\varepsilon$ model. From these two quantities can be formed a lengthscale ($L = k^{3/2}/\varepsilon$), a timescale ($\tau = k/\varepsilon$), a quantity of dimension $n_T(k^2/\varepsilon)$ . As a consequence, two-equation models can be complete-flow-dependent specifications such as a mixing length ($l_m(x)$) are not required [20].

The two transport equations are the following:

$$\frac{\partial k}{\partial t} = \nabla \cdot \left( \frac{\nu_T}{\sigma_k} \nabla k \right) + P - \varepsilon$$ (5.19)

$$\frac{\partial \varepsilon}{\partial t} = \nabla \cdot \left( \frac{\nu_T}{\sigma_\varepsilon} \nabla \varepsilon \right) + C_{\varepsilon 1} \frac{P \varepsilon}{k} - C_{\varepsilon 2} \frac{\varepsilon^2}{k}$$ (5.20)

Where $k$ is the turbulent kinetic energy, $\varepsilon$ turbulent dissipation rate, $P$ is the turbulence production, $\nu_T$ is the turbulent viscosity, and $\sigma_k$ the turbulent Prandtl number.

The standard values of all model constants are

$$C_\mu = 0.09, \quad C_{\varepsilon 1} = 1.44, \quad C_{\varepsilon 2} = 1.92, \quad \sigma_k = 1.0, \quad \sigma_\varepsilon = 1.3$$ (5.21)
Chapter 6: Fluidized Bed Simulation

The work done in this research was divided into two parts. The first part corresponds to the investigation of fluidized bed with spherical particles. The second part involves the investigation of fluidization with non-spherical particles. To simplify the complexities involved in obtaining the solution of the modeling equations, the following assumptions were made:

a) The fluid simulation domain was assumed to be centered at the bottom of the vessel containing the particles.

b) An Eulerian-Eulerian approach for both the fluid and the solid phase was considered for the simulation.

For the first study two spherical drag correlations were compared to the Ergun equation and experimental data for validation of the numerical model. The theoretical correlations employed in order to predict and compare fluidization conditions with spherical particles were:

1. Syamlal and O’Brien drag correlation, according to Equation (5.5).
2. Gidaspow drag correlation, according to Equation (5.11).

For the investigation of non-spherical particles, the work is divided into three sections:

1. The implementation of a non-spherical drag correlation found in literature, as presented in Hölzer and Sommerfeld (Hölzer and Sommerfeld, 2008).
2. The calculation of drag coefficient of a solid non-spherical particle moving at the terminal velocity is being studied. The numerical approximations are done using the solver FLUENT on a collocated grid. The non-spherical particle shape simulated in this study was elliptical. Experimental drag results are compared to experimental data for validation.
3. The derivation of a simple correlation formula for the standard drag coefficient of arbitrary shaped particles using a large number of experimental data specifically recorded for this work. This new correlation formula accounts for the particles sphericity (shape coefficient) over an
entire range of Reynolds numbers up to the critical Reynolds number. Such a correlation was used for CFD fluidized hydrodynamic modeling in uniform flow.

6.1 Spherical Particles Modeling

The experimental test bed consists of:

- 1mm ($d_p$) spherical particles.

The particles are made of Borosilicate glass which is widely used for laboratory glassware. Table 3 shows the physical properties of Borosilicate glass. The particles are contained in a cylindrical vessel of specific diameter and height. For the computational analysis only a portion of the vessel height is considered since the actual height of the vessel is larger compared to that of the bed. In addition, a static bed height was determined in order to perform the investigation. As shown in Fig. 6.1-a). The fluid simulation domain consists of a two-dimensional rectangular system (12 cm x 50 cm) with the origin of the $x$, $y$- axis centered at the left bottom corner of the rectangle.
For this investigation, a set of computational grids are generated in both FLUENT and MFX in order to achieve particular grid independence. The first computational grid was a coarse mesh with 1200 cells. Next grid was 4800 cells, the third 24200 cells, another 64400 cells and a last of 100625 cells. By checking the pressure values it was observed that after the 64400 cell-grid the results were within a 2% deviation; however the computational time increases as the number of cells increases. Thus, a last computational grid was generated but now containing a finer mesh only in the particle bed region, and axially growing coarser by a factor of 0.2, this grid was 35420 cells. The working fluid is air at isothermal condition. The fluid properties are obtained at 25 °C, with density of 1.2 kg/m$^3$, dynamic viscosity of 1.8e$^{-05}$ Pa-s. The particles bed has an initial height of 5.5 cm; this bed height was utilized for all the simulations and validation performed in this paper. For MFX, the bed was divided into a bed section and a freeboard section with the former taking up the bottom half of the bed space, as shown in Fig. 6.1-b). For MFX, the gas void fraction was set to a typical value at minimum fluidization. The gas velocity is initially set in the $y$-direction. In the freeboard section the void fraction is initially set to unity and the $y$-component of the gas velocity is initially set to value higher than the one attained at inlet velocity (typically a factor of 4 is accurate).

Table 3: Borosilicate glass physical properties (Vogel, 1994)

<table>
<thead>
<tr>
<th>Physical Properties</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>SiO$_2$ = 80.6%</td>
<td>Coefficient of expansion (20°C–300°C) 3.3 x 10$^{-6}$ K$^{-1}$</td>
</tr>
<tr>
<td>B$_2$O$_3$ = 13.0%</td>
<td>Density 2.23g/cm$^3$</td>
</tr>
<tr>
<td>Na$_2$O = 4.0%</td>
<td>Refractive index (Sodium D line) 1.474</td>
</tr>
<tr>
<td>Al$_2$O$_3$ = 2.3%</td>
<td>Dielectric constant (1MHz, 20°C) 4.6</td>
</tr>
<tr>
<td>Optical Information</td>
<td>Specific heat (20°C) 750J/kg°C</td>
</tr>
</tbody>
</table>

The values for the initial and boundary conditions for both bed and freeboard sections are shown in Table 4. In order to produce fluidization curves, most simulations were run with inlet conditions that
varied with time. For the initial conditions in FLUENT, the bed is divided into a “bed” region and a “freeboard” region with the former taking up the bottom half of the bed and the latter comprising the top half. In the bed region, the solids void fraction is initially set to 0.63, since Fluent handles solids volume fraction instead of gas volume fraction as MFIX. The gas velocity is initially set to 5 cm/s in the axial direction. The boundary conditions for the gas phase consist of no-slip, impermeable walls on the vertical sides of the bed. For the outflow boundary condition at the top of the bed, a Pressure Outlet set at atmospheric pressure (101325 Pa) is specified across the entire width. At the bed inlet, a velocity inlet boundary condition is specified.

Table 4: MFIX simulation parameters

<table>
<thead>
<tr>
<th>MFIX initial conditions</th>
<th>MFIX boundary conditions</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Bed Section</strong></td>
<td><strong>Pressure Outlet</strong></td>
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<tr>
<td>Gas Void Fraction ( \varepsilon_g )</td>
<td>0.37</td>
</tr>
<tr>
<td>Gas Velocity ( \nu_g )</td>
<td>5 cm/s</td>
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<tr>
<td>Inlet Gas Void Fraction ( \varepsilon_g )</td>
<td>1.0</td>
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</table>

<table>
<thead>
<tr>
<th>Freeboard Section</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gas Void Fraction ( \varepsilon_g )</td>
</tr>
<tr>
<td>Gas Velocity ( \nu_g )</td>
</tr>
</tbody>
</table>

6.2 Non-Spherical Particles Modeling

6.2.1 Literature Non-Spherical Drag Correlation

The non-spherical correlation implemented into FLUENT and MFIX depends on the shape and orientation, for the sake of this analysis the equation was modified to only take into account the shape of particles:

\[
C_{D_{-\text{non\-spherical}}} = \frac{24}{Re} \frac{1}{\sqrt{\phi}} + \frac{3}{\sqrt{Re}} \frac{1}{\phi^{3/4}} + 0.421 \times 10^{0.4(-\text{Log} \ \phi)^{0.2}} \frac{1}{\phi} \quad (6.1)
\]
The sphericity $\phi$ represents the ratio between the actual particle volume and that of the equivalent sphere. In order to characterize the non-spherical particles for comparison to spherical particles the sphericity was used. The sphericity was calculated using the expressions shown below (Boggs, 1967):

$$\phi = \frac{3 \sqrt[3]{\text{Particle Volume}}}{\sqrt[3]{\text{Circumscribed Sphere Volume}}}$$

(6.2)

In order to calculate the sphericity of a particle, a tri-axial ellipsoid having three diameters was imposed on the surface of the particle being investigated. An example of the three lengths used for a non-spherical particle in this study is shown in Fig. 6.2. Substitution of these lengths into Eqn. (11), results in the following:

$$\phi = \frac{3 \sqrt{bc}}{a^2}$$

(6.3)

![Figure 6.2: Actual photograph showing sphericity analysis of a non-spherical particle](image)

The non-spherical particles have the following parameters:

- 0.85 mm ($d_m$) and sphericity of 0.55 non-spherical particles.
Furthermore, the CFD modeling is carried out in the exact same way as for spherical particles (same Initial and Boundary Conditions), although for the non-spherical analysis a modification to the codes (FLUENT and MFIX) was made in order to take into account the non-spherical drag correlation. Both codes only deal with drag correlations designed for spherical particles. Thus a sub-routine written in C++ language was implemented into the Codes. By using Eqn. (5.5), the Syamlal-O'brien drag correlation as baseline, the drag coefficient was changed from that of Eqn (5.6), Dalla Valle to the one of Eqn. (6.1), the Hölzer and Sommerfeld equation. The non-spherical drag correlation sub-routine is described in the Appendix.

6.2.2 Single Non-Spherical Particle Drag Analysis

For the numerical simulation a rice grain was modeled. The shape was approximated as that of an ellipsoid as shown in Figure 6.3. The following semi-axis parameters were set to be the same as the rice grain used in the experimental portion of the results where a= 3.38 mm, b= 1.04 mm and c= 0.86 mm. The rice grain density ($\rho_s$) was determined to be 577 kg/m$^3$, and particle mass ($m_s$) was determined to be 2.33 mg using a high accuracy digital mass scale.
In order to calculate the terminal velocity of the particle an analysis was performed on the non-spherical particle. The particle was assumed to fall under the influence of gravity with other forces acting on the particle including buoyancy and drag. A force balance results in:

\[ W = F_b + D \]  

(6.4)

For the ellipsoidal shape:

\[ W = m_s g = \frac{4}{3} \pi abc \rho_s g \]  

(6.5)

\[ F_b = \frac{4}{3} \pi abc \rho_f g \]  

(6.6)

\[ D = C_D \frac{1}{2} \rho_f v_f^2 A \]  

(6.7)

Where \( g = 9.81 \text{ m/s}^2 \), \( \rho_s \) = density of the fluid (air) = 1.22 kg/m\(^3\), \( A = \pi ac \), and was initially assumed as \( C_D = 0.6 \) which is the drag force acting on the surface of an elliptical cylinder at comparable Reynolds numbers.
Substitution of Eqns. (6.5-7) in Eqn. (6.4) and solving for the terminal velocity, $v_t$, yields the following expression:

$$v_t = \sqrt{\frac{8 b g (\rho_s - \rho_f)}{3 C_D \rho_f}}$$  \hspace{1cm} (6.8)

The value of $v_t$ with these assumptions was initially determined to be 4.6 m/s. This provided a starting value of the velocity needed for the test to be performed. The terminal velocity was later determined during the simulation.

The particle velocity was used to calculate a Reynolds number based on the largest semi-axis length of the ellipsoid in this case $a$, where the viscosity of the fluid $\mu_f$ is taken to be $1.8 \times 10^{-5}$ kg/m-s:

$$Re = \frac{\rho_f v_s a}{\mu_f}$$  \hspace{1cm} (6.9)

The particle drag coefficient was also calculated with the following equation:

$$C_D = \frac{F}{2 \rho_f v_s^2 A}$$  \hspace{1cm} (6.10)

a) Numerical Modeling

The numerical approximations were achieved using the solver FLUENT. The parameters defined in the previous section were used in the software for the model. The model was analyzed assuming the non-spherical element was set to move downwards at free-falling conditions, and a moving mesh was used. In order to test possible moving mesh methods, several grid configurations were used for the analysis. The assumption used for all the simulations was a two-dimensional domain. The boundary conditions and mesh dimensions are labeled in Figure 6.4. A moving wall condition is assigned to boundary 1 and a no-slip wall condition assigned to boundary 4 while a pressure-outlet condition was set for boundaries 2, 3 and 5.
Figure 6.4: Grid domain and boundary conditions

For the moving mesh analysis additional parameters were calculated. The translation and possible rotation of the non-spherical particle, the degrees of freedom, and the deformation of the elements were done using a User Defined Function (UDF). The parameters concerning the particle are considered including: the mass of the particle and the mass-moments of inertia.

The following equations present the mass moment of inertia calculations about three axes:

\[
I_{zz} = m_s \left(\frac{a^2 + b^2}{5}\right) = 5.818 \times 10^{-12} \text{ kg-m}^2 \tag{6.11}
\]

\[
I_{yy} = m_s \left(\frac{c^2 + a^2}{5}\right) = 5.66 \times 10^{-12} \text{ kg-m}^2 \tag{6.12}
\]

\[
I_{xx} = m_s \left(\frac{b^2 + c^2}{5}\right) = 8.47 \times 10^{-13} \text{ kg-m}^2 \tag{6.13}
\]
The first moving mesh was then tested, and the particle was simulated to fall for 10 ms with a time step of 0.01 ms, for this grid the elements around the particle were also deforming and output non-constant values for the elements surrounding the particle. Thus, the first mesh was not used. For next tested mesh modifications were made and a constant-size region of elements surrounding the particle was created. The chosen elements for this region were quadrilateral elements, as shown in Figure 6.5. Some uneven distortion was still appreciated in the triangular elements surrounding the quad-element particle region, especially in the corners, since it is a rectangular region.

![Figure 6.5: Grid with particle rectangular-constant-size quad elements region](image)

The third grid was modified to have an elliptical constant element-size region surrounding the particle, as shown in Figure 6.6, with this change a more reliable element distortion and remeshing was achieved. For this reason this grid was chosen for the moving mesh analysis.

![Figure 6.6: Grid with particle elliptical-constant-size quad elements region](image)
6.2.3 Experimental Non-Spherical Drag Correlation

In this section, an experimental investigation is performed in order to develop a correlation of drag coefficient as a function of Reynolds number for non-spherical particles of a specific sphericity. In addition this drag correlation is implemented in a computational model for gas-solid fluidized bed with non-spherical particles in uniform flow.

This study was based on the general drag correlation proposed by Haider and Levenspiel (Haider and Levenspiel, 1989), all of which happen to contain 4 arbitrary constants, as described in Eqn. (6.14):

\[
C_D = \frac{24}{Re} \left( 1 + A R e^B \right) + \frac{C}{1 + \frac{D}{Re}}
\]  
(6.14)

This drag correlation is used in order to fit the non-spherical experimental data specifically recorded for this work. A non-linear least squares numerical technique is performed and in conjunction with a Newton-Raphson iterative scheme and the following equation was developed fitting the non-spherical experimental data.

The non-spherical particles have the following parameters:

- 1.15 mm (d_m) and sphericity of 0.55 non-spherical particles.

Furthermore, the CFD modeling is carried out in the exact same way as for spherical particles (same Initial and Boundary Conditions), although for the non-spherical analysis a modification to the codes (FLUENT and MFIX) was made in order to take into account the non-spherical drag correlation. Both codes only deal with drag correlations designed for spherical particles. Thus a sub-routine written in C++ language was implemented into the Codes. By using Eqn. (5.5), the Syamlal-O’brien drag correlation as baseline, the drag coefficient was changed from that of Eqn (5.6), Dalla Valle to the one
numerically found through the fit given by Eqn. (6.14). The non-spherical drag correlation sub-routine is described in the Appendix.

6.3 Theoretical Correlation Validation

By using the theoretical correlation found in Equation (4.29), based on the pressure drop principles, the minimum fluidization was calculated and compared with those found on the simulations, the equation commonly known as the “Ergun equation”. Also, the predictive results using the Ergun equation are presented alongside the numerical results obtained when using the other drag models.
Chapter 7: Experimental Setup

7.1 Spherical and Non-Spherical Particles

The following setup description was used for all the experimental validation involving fluidized bed behavior, including both spherical and non-spherical particles. The setup is composed of 2 primary sections: a column section and a fluid delivery section (Fig. 7.1). The lower portion of the column section is made of Plexiglas with 12.7 cm outer diameter and 0.318 cm wall thickness. At the bottom portion the Plexiglas section a flow straightener made of ABS plastic is used to uniform distribution of air through the test section. Immediately above this section a mesh catch with 0.053 mm of nominal diameter is used to ensure that the particles remain in the test section. A quartz tube with 12 cm outer diameter and 0.5 cm wall thickness is inserted into the Plexiglas portion and extends up 2m. 1 mm spherical borosilicate glass beads are placed at a height of 5.5 cm in the test section and are assumed to have a sphericity of 1.

To measure pressure drop across the test bed a digital display manometer (Omega HHP4252 with 7 Pa resolution) is used. The fluid delivery section uses Grainger 3.7 kW high-pressure blower to supply air to the test section of packed bed column, a wafer type butterfly valve with 12.7 cm diameter and 1 cm thick flange is used. The butterfly valve is made of cast iron and rated for the pressures and temperatures appropriate to this experiment. Volumetric flow rate is measured using an insertion type thermal mass flow meter with 200 ms response time.
A high-speed camera system, maximum frame of 20,000 frames per second, was used to record particle movement at the base and near the top the fluidized bed. Imaging was acquired at (a) minimum fluidization, (b) transition, and (c) terminal velocity. An example of the particle imaging captured at large (entire bed) and small (individual particles) scales is presented in Fig. 7.2-a). At the terminal velocity condition the camera position on the column was determined based on the maximum height attained (in average) by the particles when lifted by the compressed air.
Figure 7.2: a) High-speed particle motion b) Magnified photographs of spherical particles, and non-spherical particles

Moreover, the particle size characterization technique was performed in the following way. Spherical particles assumed sphericity value of 1.0. The non-spherical particles were obtained by crushing 6 mm borosilicate glass beads using a compression machine. Figure 7.2-b) shows a magnified image of both the spherical particles and non-spherical particles captured using a video camera. After crushing beads into the non-spherical particles, a sieve test technique was done to separate the particles by size. Taking the images obtained of the particles a sphericity analysis was performed for a number of individual particles using Eqn. (6.3). The particle sphericity was found in the range of 0.50 to 0.60. Thus, the average 0.55 was considered for the numerical analysis. An individual particle with 0.55 sphericity value was presented in Fig. 6.2 which showed the three diameters (intercepts) of a, b and c. Results showed that the non-spherical particles used in this experiment ranged from 0.9 to 2.0 mm with mean particle size of 1.5 mm.
7.2 Single Non-Spherical Particle Analysis and Non-Spherical Drag Correlation

The following procedure was used in order to predict drag coefficient for non-spherical particles. Both the single particle and the non-spherical drag correlation followed the same methodology for finding drag and Reynolds number data. In addition, the same high-speed camera system as previously described was used capable of recording up to 500 kHz, it captured the particle motion in the free falling stream as shown in Figure 7.3. A single particle motion was captured at a height of 2.2 m from the top of the bed at a rate of 3100 frames per second. A digital image analyzing software Phantom was used to track the particle motion frame by frame from the videos obtained by the high speed camera. The software was used to track the starting and ending point of the free falling particle in the camera frame, and also to track the time required to travel that distance by a single particle. Figure 7.4 shows the motion captured for a falling particle at terminal velocity at 4 intervals of time.

The particle terminal velocity was obtained using Eq. (7.1):

\[ V_s = \frac{\Delta S}{\Delta t} \]  

(7.1)

Where \( \Delta s \) is the distance travelled and \( \Delta t \) is the time required.

Finally, the experimental drag coefficient for a single rice grain was calculated using Eqn. (6.8) and solving for \( C_D \):

\[ C_D = \frac{8}{3} b g (\rho_s - \rho_f) \frac{\rho_f v_s^2}{\rho_f v_s^2} \]  

(7.2)
Figure 7.3: Experimental setup

Figure 7.4: Particle motion captured with high-speed camera
Chapter 8: Results and Discussion

8.1 Spherical Particles

Bubbling behavior in the fluidized bed takes place in a transitory way, where splitting and collapsing of bubbles occur, due to this, fluctuations in the pressure drop are anticipated. In line to this, area-weighted average values of pressure drop values are recorded providing a comparison between simulation results. Consequently, time-averaging was carried out over a range of 1–10 seconds of time computation. The first set of simulations was performed using FLUENT with spherical particles, the pressure drop variation inside the bed as the superficial gas velocity increases using the Syamlal-O’Brien and Gidaspow drag models is shown in Fig. 8.1, where numerical values are compared with the experimental and theoretical findings. The plot describes a typical fluidized bed behavior. Where a linear increase of pressure with respect to superficial velocity is seen, also known as packed-bed behavior, until the inflow gas velocity reaches what is known as the minimum fluidization velocity $U_{mf}$, also the pressure drop reaches a maximum pressure drop value, theoretically this maximum pressure drop value should be equal to the weight of the bed per cross-sectional area of the vessel containing the particles.
Additionally, this pressure drop value remains near continuous showing a relative linear trend with increasing gas velocity once the fluidization point has been reached. As appreciated in Fig. 8.2, MFIX drag models describe with good accuracy the packed-bed behavior with respect to the theoretical and experimental results as well, where a linear increase of pressure with respect to superficial velocity is appreciated, reaching later on the minimum fluidization velocity. In addition, this pressure drop value remains nearby constant showing a comparative linear development with increasing gas velocity, as seen before with the FLUENT results. By further increasing the inflow velocity the established constant pressure drop starts to fluctuate, due to the constant bubbling behavior of the bed. At this instance, FLUENT and MFIX numerical results describe somewhat higher values than the experimental results for both drag models.
The validation of the model with spherical particles was done in several steps. The numerical codes were tested for numerical convergence. The methods were stable and converged with the set time step size. The fluid-particle interaction was compared with empirical solutions and experimental observations. Table 5 demonstrates the very good agreement of the measured pressure drop through a fluidized bed (at packed conditions no particle movement is observed since the flow speed is below the minimum fluidization velocity) with the predictions of Ergun’s empirical equation and the experimental findings for spherical particles.

![Graph](image_url)

**Figure 8.2: MFIX spherical particles validation with experimental results**
Table 5: Numerical, theoretical and experimental results for spherical particles

<table>
<thead>
<tr>
<th></th>
<th>FLUENT</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Drag Correlation</td>
<td>Min. Fluidization Velocity (cm/s)</td>
<td>Pressure Drop (Pa)</td>
</tr>
<tr>
<td>Syamlal-O’Brien</td>
<td>43</td>
<td>755.7</td>
</tr>
<tr>
<td>Gidaspow</td>
<td>43</td>
<td>754.6</td>
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<table>
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<td>Min. Fluidization Velocity (cm/s)</td>
<td>Pressure Drop (Pa)</td>
</tr>
<tr>
<td>Syamlal-O’Brien</td>
<td>43</td>
<td>755.0</td>
</tr>
<tr>
<td>Gidaspow</td>
<td>43</td>
<td>753.2</td>
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<table>
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<td>Correlation</td>
<td>Min. Fluidization Velocity (cm/s)</td>
<td>Pressure Drop (Pa)</td>
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<td>Ergun</td>
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<table>
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<tr>
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<th>EXPERIMENTAL</th>
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<tbody>
<tr>
<td>Min. Fluidization Velocity (cm/s)</td>
<td>Pressure Drop (Pa)</td>
<td></td>
</tr>
<tr>
<td>43.7</td>
<td>743.0</td>
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</table>

In order to provide a more precise understanding about the fluidization hydrodynamics, instantaneous gas and solid flow contours were recorded from within FLUENT and MFIX. Flow fields of the axial component of gas velocity at simulated flow time of 1.5 s are given in Fig. 8.3 for spherical particles. Bubbling bed behavior is observed as the flow develops through the gas void between the solid particles, both codes for Syamlal–O’Brien as well as for Gidaspow’s drag function show similar behavior. Also, the solid-phase velocity vectors are shown in Fig. 8.4 and a very good agreement between FLUENT and MFIX and numerical results is appreciated. In addition, Fig. 8.5 shows the solids volume fraction profile for inflow velocity of 75 cm/s at 1.5 s simulation time, no significant pattern differences exist among the gas volume fraction contours shown in FLUENT and MFIX. Numerical results of MFIX and Fluent are quite similar for both drag models.
Figure 8.3: Snapshots of gas-axial velocity at 75 cm/s inflow velocity with spherical particles

Figure 8.4: Snapshots of solids velocity vector-field for inflow velocity of 75 cm/s with spherical particles
The qualitative comparison is made in Fig. 8.6 by displaying some demonstrative snapshots from computational work and experiment at different times. While in the numerical simulation snapshots is appreciated the development of colliding and collapsing bubbles as the gas is being increasingly supplied at the bottom of the bed, the colors red and light blue indicate the volume fraction of solids in the fluidization domain, being red a high fraction of solid particles, while blue is the presence of air voids and bubbles forming in the bed. The experimental snapshots present a similar bubbling behavior, showing a high accurate qualitative comparison with respect to the numerical simulations. In both experiment and simulation it is observed that, beginning from a well mixing state, a series of bubbles starting to form at the bottom of the bed and colliding at the top, the bubble formation increases with higher gas flow as time progresses. Realistic agreement between experiment and simulation can be obtained from this comparison.
Figure 8.6: Comparison of snapshots of bubbling behavior of spherical particles among simulation (top row) and experiment (bottom row) at t= 2, 5, 7 s from left to right
8.2 Non-Spherical Particles

8.2.1 Literature Drag Correlation

On the other hand, another set of simulation was performed in order to obtain results and predictions for non-spherical particles. The pressure drop variation inside the bed as the superficial gas velocity increases using the Hölzer and Sommerfeld drag model is shown in Fig. 8.7, where both numerical values for FLUENT and MFI X are compared with the experimental and theoretical findings. The plot describes a typical fluidized bed behavior. Where a linear increase of pressure with respect to superficial velocity is seen, also the pressure drop reaches a maximum pressure drop value, furthermore, this pressure drop value remains near continuous showing a relative linear trend with increasing gas velocity once the fluidization point has been reached, however as the inflow gas velocity increases it reaches a point where pressure drop slightly increases once again.

![Fluidization (5.5 cm Bed, 0.85-1 mm, sphericity 0.55)](image)

Figure 8.7: Non-spherical particles fluidization curves from simulations results, theoretical approximation and experimental predictions
As appreciated in Fig. 8.7, both FLUENT and MFIX drag models describe this behavior accurately, showing a good agreement with the experimental findings. As a result the non-spherical behavior differs from the spherical one at higher inflow velocity values, particularly showing a significant difference with respect to the theoretical non-spherical predictions. Table 6 shows results for non-spherical particles, the results deviate from Ergun equation for less than 10%.

Table 6: Non-spherical numerical, theoretical and experimental results

<table>
<thead>
<tr>
<th></th>
<th>FLUENT</th>
<th>MFIX</th>
</tr>
</thead>
<tbody>
<tr>
<td>Drag Correlation</td>
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<td>Hölzer-Sommerfeld</td>
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<tr>
<td>Min. Fluidization Velocity (cm/s)</td>
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<td>28.0</td>
</tr>
<tr>
<td>Pressure Drop (Pa)</td>
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<td>THEORETICAL</td>
<td>Ergun</td>
<td></td>
</tr>
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<td>Min. Fluidization Velocity (cm/s)</td>
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<td></td>
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<td>Pressure Drop (Pa)</td>
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<td></td>
</tr>
<tr>
<td>EXPERIMENTAL</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Min. Fluidization Velocity (cm/s)</td>
<td>32.41</td>
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</tr>
<tr>
<td>Pressure Drop (Pa)</td>
<td>476.0</td>
<td></td>
</tr>
</tbody>
</table>

Lastly, to provide a more precise understanding about the fluidization hydrodynamics, instantaneous gas and solid flow contours were recorded from within FLUENT and MFIX for non-spherical particles. Flow fields of the axial component of gas velocity at simulated flow time of 1.5 s are given in Fig. 8.8. Bubbling bed behavior is observed as the flow develops through the gas void between the solid particles. Also, the solid-phase velocity vectors are shown in Fig. 8.9 and a very good agreement between FLUENT and MFIX and numerical results is appreciated. In addition, Fig. 8.10 shows the solids volume fraction profile for inflow velocity of 75 cm/s at 1.5 s simulation time, no significant pattern differences exist among the gas volume fraction contours shown in FLUENT and MFIX. Numerical results of MFIX and Fluent are comparable.
Figure 8.8: Snapshots of gas-axial velocity at 75 cm/s inflow velocity with non-spherical particles

Figure 8.9: Snapshots of solids velocity vector-field for inflow velocity of 75 cm/s with non-spherical particles
Figure 8.10: Snapshots of solid-phase vol. fraction for inflow velocity of 75 cm/s with non-spherical particles
8.2.2 Single Non-Spherical Particle Analysis

A. Numerical

In order to validate the model, particle velocity results were obtained using FLUENT, and contrasted with those found in Eqn. (6.8). Figure 8.11 shows the particle velocity plot, a 2% error was found between numerical results compared with those found by the theoretical calculation for terminal velocity. Figure 8.12 presents contours of velocity for the particle at different times.

![Particle Velocity](image)

Figure 8.11: Particle velocity results
Figure 8.12: Velocity contours at different times

Figure 8.13 displays the force acting on the particle at the free-falling conditions, a fluctuation is observed due to the vortices acting on the particle.

Figure 8.13: Fluid force acting on the particle
Equations (6.9-10) were used to calculate the particle drag coefficient at terminal velocity, a comparison between numerical and experimental results can be appreciated in Table 7:

<table>
<thead>
<tr>
<th>Results</th>
<th>Numerical</th>
<th>Experimental</th>
</tr>
</thead>
<tbody>
<tr>
<td>Re</td>
<td>1058</td>
<td>1081</td>
</tr>
<tr>
<td>Cd</td>
<td>0.52</td>
<td>0.58</td>
</tr>
</tbody>
</table>

**B. Experimental**

The initial terminal velocity for determining the approximate particle travel distance was calculated. The camera frame length traveled by a single particle, presented in Figure 7.4, was measured using an mm scale. After obtaining the travel time, the particle terminal velocity was obtained using Eq. (7.1). The terminal velocity for the present experiment was found to be approximately 4.7 m/s. The drag coefficient based on the measurement was determined experimentally using Eqn. (7.2) and was found to be approximately 0.58. The experimental uncertainty was also calculated based on a Student’s t-distribution with a 95% confidence interval and estimated to be approximately 10% of the mean value presented.

**8.2.3 Experimental Non-Spherical Drag Correlation**

In order to develop a correlation of drag coefficient as a function of Reynolds number for non-spherical particles of a sphericity 0.55, experimental data was performed as described in previous sections, and 93 experimental data points were recorded for Re < 1000, as presented in the Appendix.

By considering the general drag correlation proposed described in Eqn. (6.14), this relationship is used in order to fit the non-spherical experimental data previously termed in this work. As a consequence, a non-linear least squares numerical technique is performed in conjunction with a Newton-
Raphson iterative scheme and the following equation is developed fitting the non-spherical experimental data:

\[
C_D = \frac{24}{Re} \left( 1 + 0.8943 Re^{0.3952} \right) + \frac{4.3215}{1 + \frac{160.1567}{Re}}
\]  

(8.1)

Figure 8.14 describes the drag coefficient vs. Reynolds number, for both the experimental data and the correlation found through non-linear fit.

Finally, the goodness of fit of Eqn. (8.1) is quantified using the RMS deviation. RMS deviation measures the average fractional displacement of the measured \( C_D \) values from the correlation line:

\[
RMS = \sqrt{\frac{\sum_{i=1}^{n} (\log_{10}(C_{D,\text{exp}}) - \log_{10}(C_{D,\text{cal}}))^2}{n}}
\]  

(8.2)

Where the RMS values for this correlation is equal to 0.048.
Furthermore, the fluidization of non-spherical particles is performed next, by using this experimentally developed drag correlation. First, by using Eqn. (5.5), the Syamlal-O’brien drag correlation as baseline, the drag coefficient was changed from that of Eqn (5.6), Dalla Valle to the one numerically found through the fit given by Eqn. (8.1). Next, for this CFD non-spherical analysis a modification to the codes (FLUENT and MFIX) was made in order to take into account the newly developed non-spherical drag correlation. Both codes only deal with drag correlations designed for spherical particles. Thus a sub-routine written in C++ language was implemented into the Codes. The non-spherical drag correlation sub-routine is described in the Appendix.

The results acquired by the CFD codes describe a bubbling behavior in the fluidized bed that takes place in a transitory way, where splitting and collapsing of bubbles occur, due to this, fluctuations in the pressure drop are anticipated. In line to this, area-weighted average values of pressure drop values are recorded providing a comparison between simulation results. Consequently, time-averaging was carried out over a range of 1–10 seconds of time computation. The simulations was performed using FLUENT with non-spherical particles, the pressure drop variation inside the bed as the superficial gas velocity increases is shown in Fig. 8.15, where numerical values are compared with the experimental and theoretical findings. The plot describes a typical fluidized bed behavior. Where a linear increase of pressure with respect to superficial velocity is seen, also known as packed-bed behavior, until the inflow gas velocity reaches what is known as the minimum fluidization velocity $U_{mf}$, also the pressure drop reaches a maximum pressure drop value, theoretically this maximum pressure drop value should be equal to the weight of the bed per cross-sectional area of the vessel containing the particles.

Additionally, this pressure drop value remains near continuous showing a relative linear trend with increasing gas velocity once the fluidization point has been reached. As appreciated in Fig. 8.15, MFIX results describe with good accuracy the packed-bed behavior with respect to the theoretical
and experimental results as well, where a linear increase of pressure with respect to superficial velocity is appreciated, reaching later on the minimum fluidization velocity. In addition, this pressure drop value remains nearby constant showing a comparative linear development with increasing gas velocity, as seen before with the FLUENT results. By further increasing the inflow velocity the established constant pressure drop starts to fluctuate, due to the constant bubbling behavior of the bed. At this instance, FLUENT and MFIX numerical results describe somewhat smaller values than the experimental results for both numerical codes.

![Fluidization graph](image)

Figure 8.15: Non-spherical particles fluidization curves from simulations results, theoretical approximation and experimental predictions

The validation of the model with non-spherical particles was done in several steps. The numerical codes were tested for numerical convergence. The methods were stable and converged with
the set time step size. The fluid-particle interaction was compared with empirical solutions and experimental observations. Table 8 demonstrates the very good agreement of the measured pressure drop through a fluidized bed (at packed conditions no particle movement is observed since the flow speed is below the minimum fluidization velocity) with the predictions of Ergun’s empirical equation and the experimental findings for non-spherical particles. The results deviate from Ergun equation for less than 10%.

Table 8: Non-spherical numerical, theoretical and experimental results

<table>
<thead>
<tr>
<th></th>
<th>FLUENT</th>
<th>MFIX</th>
<th>THEORETICAL</th>
<th>EXPERIMENTAL</th>
</tr>
</thead>
<tbody>
<tr>
<td>Min. Fluidization Velocity (cm/s)</td>
<td>Pressure Drop (Pa)</td>
<td>Pressure Drop (Pa)</td>
<td>Pressure Drop (Pa)</td>
<td>Pressure Drop (Pa)</td>
</tr>
<tr>
<td>30.5</td>
<td>450.5</td>
<td>31.0</td>
<td>463.2</td>
<td>26.52</td>
</tr>
<tr>
<td>31.0</td>
<td>463.2</td>
<td>26.52</td>
<td>512</td>
<td>32.41</td>
</tr>
</tbody>
</table>

In order to provide a more precise understanding about the fluidization hydrodynamics, instantaneous gas and solid flow contours were recorded from within FLUENT and MFIX. Flow fields of the axial component of gas velocity at simulated flow time of 1.5 s are given in Fig. 8.16 for non-spherical particles. Bubbling bed behavior is observed as the flow develops through the gas void between the solid particles, both codes show similar behavior. Also, the solid-phase velocity vectors are shown in Fig. 8.17 and a very good agreement between FLUENT and MFIX numerical results is
appreciated. In addition, Fig. 8.18 shows the solids volume fraction profile for inflow velocity of 75 cm/s at 1.5 s simulation time, no significant pattern differences exist among the gas volume fraction contours shown in between FLUENT and MFIX.

Figure 8.16: Snapshots of gas-axial velocity at 75 cm/s inflow velocity with non-spherical particles
Figure 8.17: Snapshots of solids velocity vector-field for inflow velocity of 75 cm/s with non-spherical particles
Figure 8.18: Snapshots of solid-phase vol. fraction for inflow velocity of 75 cm/s with non-spherical particles
Chapter 9: Conclusions

This study established a predictive method by which the hydrodynamics of a 2D fluidized bed can be documented for both spherical and non-spherical particles. This investigation offers an experimental study and simulation of multiphase flow in a fluidized bed. The behavior of spherical drag models, specifically the Syamlal-O’Brien and Gidaspow models on CFD numerical modeling of a 2D fluidized bed is investigated. Two CFD codes are used: the commercial software FLUENT and the open-source MFIX, developed by the DOE. MFIX and FLUENT results are compared between themselves for gas inflow velocities up to 130 cm/s. Also, the simulation of fluidized bed behavior with non-spherical particles is carried out. First, the Hölzer and Sommerfeld drag law found in literature is used for studying non-spherical particles. The non-spherical particles are developed by crushing bigger particles. Both spherical and non-spherical particle fluidizations curves are presented in this work. For the spherical particles portion of the investigation, the FLUENT code numerical results show a deviation less than 1.5% between the Gidaspow and Syamlal-O’Brien spherical drag laws, also less than 2% deviation with respect to the Ergun theoretical equation. MFIX results are found to be between the 2.5% deviation with respect to the Ergun equation. Moreover, both FLUENT and MFIX codes correlate within 3% deviation with experimental findings. For the literature non-spherical drag law study, deviation is found for both pressure drop and minimum fluidization velocity. As for the FLUENT results with respect to Ergun equation a 6% is found for pressure drop while 17% for minimum fluidization velocity. MFIX has a 7% deviation for pressure drop and 5.6% for minimum fluidization velocity. If it is now compared the error found between experimental and numerical results, it is found that FLUENT deviation is 0.8% for pressure drop and 4.3% for minimum fluidization velocity. MFIX has a 0.2% and 13.6% for pressure drop and minimum fluidization velocity. Thus, for this portion of the study the numerical results have a better correlation with those found experimentally rather than the theoretical non-spherical Ergun equation.
Moreover, the calculation of drag coefficient of a single solid non-spherical particle moving at the terminal velocity is studied. The numerical approximations were done using FLUENT. The non-spherical particle shape simulated in this study is a rice grain shaped as an ellipsoid. Experimental drag results are compared to experimental data for validation. The experimental setup is comprised of an elliptical rice particle and a high-speed camera system, with a capacity up to 500 kHz, used to record particle movement in the free falling stream to determine the terminal velocity of the rice grain. Drag coefficient is successfully modeled through CFD methodologies; in addition the numerical work is validated with an experimental method developed specifically for these measurements. The deviation between numerical and experimental work is less than 7%.

Finally, this study established an experimental simple correlation formula for the standard drag coefficient of arbitrary shaped particles is established using a large number of experimental data specifically recorded for this work. This new correlation formula accounts for the particles sphericity (shape coefficient) of 0.55 over an entire range of Reynolds numbers up to the critical Reynolds number (Re <1e03). The numerically fit drag correlation has a RMS deviation of 0.048 with respect to the drag experimental measurements. In addition, such a correlation was used for CFD hydrodynamic modeling of a gas-solid fluidized bed with non-spherical particles in uniform flow. The same two CFD codes previously described are used to perform this analysis. Both CFD codes results were compared between themselves for gas inflow velocities up to 130 cm/s. Deviation was found for both pressure drop and minimum fluidization velocity. As for the FLUENT results with respect to non-spherical Ergun equation a 12% is found for pressure drop while 15% for minimum fluidization velocity. MFIX had 9% deviation for pressure drop and 16% for minimum fluidization velocity. If it is now compared the error found between experimental and numerical results, it is found that FLUENT deviation is 5.4% for pressure drop and 5.9% for minimum fluidization velocity. MFIX has a 2.7% and 4.4% for pressure drop and minimum fluidization velocity. In conclusion, the numerical results have a
better correlation with those found experimentally rather than the theoretical non-spherical Ergun equation.
References


Dolej’s, V., Machac’, I., “Pressure drop during the flow of a Newtonian fluid through a fixed bed of particles”. Chemical Engineering and Processing 34, 1995, pp. 1–8.


Glasser, B.J. "From Bubbles to Clusters in Fluidized Beds", Physical Review Letters, 1998


Li, S. "Modelling of the behaviour of gas-solid two-phase mixtures flowing through packed beds", Chemical Engineering Science, 200603.


Appendix

Table 9: User Defined Function for Syamlal-Obrien with Holzer and Sommerfeld Drag Correlation

```c
#include "udf.h"
#include "sg_mphase.h"

#define pi 4.*atan(1.)
#define diam2 1.e-3

DEFINE_EXCHANGE_PROPERTY(custom_drag_syam, cell, mix_thread, s_col, f_col)
{
    Thread *thread_g, *thread_s;
    real x_vel_g, x_vel_s, y_vel_g, y_vel_s, abs_v, slip_x, slip_y,
        rho_g, rho_s, mu_g, reyp, afac,
        bfac, void_g, vfac, fdrgs, taup, k_g_s;

    /* find the threads for the gas (primary) and solids (secondary phases).
    These phases appear in columns 2 and 1 in the Interphase panel respectively*/
    thread_g = THREAD_SUB_THREAD(mix_thread, s_col); /*gas phase*/
    thread_s = THREAD_SUB_THREAD(mix_thread, f_col); /* solid phase*/

    /* find phase velocities and properties*/
    x_vel_g = C_U(cell, thread_g);
    y_vel_g = C_V(cell, thread_g);
    x_vel_s = C_U(cell, thread_s);
    y_vel_s = C_V(cell, thread_s);
    slip_x = x_vel_g - x_vel_s;
    slip_y = y_vel_g - y_vel_s;
    rho_g = C_R(cell, thread_g);
    rho_s = C_R(cell, thread_s);
    mu_g = C_MU_L(cell, thread_g);

    /*compute slip*/
    abs_v = sqrt(slip_x*slip_x + slip_y*slip_y);

    /*compute reynolds number*/
    reyp = rho_g*abs_v*diam2/mu_g;

    /* compute particle relaxation time */
    taup = rho_s*diam2/diam2/18./mu_g;
    void_g = C_VOF(cell, thread_g); /* gas vol frac*/

    /*compute drag and return drag coeff, k_g_s*/
    afac = pow(void_g,4.14);
}
```
if (void_g<=0.85)
    bfac = 0.26*pow(void_g, 1.28);
else
    bfac = pow(void_g, 9.56872);

vfac = 0.5*(afac-0.06*reyp+sqrt(0.0036*reyp*reyp+0.12*reyp*(2.*bfac-
    afac)+afac*afac));
fdrgs = void_g*((24/sqrt(sphericity))+(3*sqrt(reyp))*(1/pow(sphericity,0.75)+
    (0.42*(pow(10,(0.4*(pow(-log(sphericity),0.2))))))*(reyp/sphericity))/
    (24.0*pow(vfac,2)));

k_g_s = (1.-void_g)*rho_s*fdrgs/taup;

return k_g_s;
Table 10: User Defined Function for Syamlal-Obrien Corrected with Experimentally Developed Drag Correlation

```c
#include "udf.h"
#include "sg_mphase.h"

#define pi 4.*atan(1.)
#define diam2 1.e-3

DEFINE_EXCHANGE_PROPERTY(custom_drag_syam, cell, mix_thread, s_col, f_col) {
    Thread *thread_g, *thread_s;
    real x_vel_g, x_vel_s, y_vel_g, y_vel_s, abs_v, slip_x, slip_y,
        rho_g, rho_s, mu_g, reyp, afac,
        bfac, void_g, vfac, fdrgs, taup, k_g_s;

    /* find the threads for the gas (primary) and solids (secondary phases). These phases appear in columns 2 and 1 in the Interphase panel respectively*/
    thread_g = THREAD_SUB_THREAD(mix_thread, s_col); /*gas phase*/
    thread_s = THREAD_SUB_THREAD(mix_thread, f_col); /* solid phase*/

    /* find phase velocities and properties*/
    x_vel_g = C_U(cell, thread_g);
    y_vel_g = C_V(cell, thread_g);

    x_vel_s = C_U(cell, thread_s);
    y_vel_s = C_V(cell, thread_s);

    slip_x = x_vel_g - x_vel_s;
    slip_y = y_vel_g - y_vel_s;

    rho_g = C_R(cell, thread_g);
    rho_s = C_R(cell, thread_s);

    mu_g = C_MU_L(cell, thread_g);

    /*compute slip*/
    abs_v = sqrt(slip_x*slip_x + slip_y*slip_y);

    /*compute reynolds number*/
    reyp = rho_g*abs_v*diam2/mu_g;

    /* compute particle relaxation time */
    taup = rho_s*diam2*diam2/18./mu_g;

    void_g = C_VOF(cell, thread_g); /* gas vol frac*/

    /*compute drag and return drag coeff, k_g_s*/
    afac = pow(void_g, 4.14);

    if(void_g<=0.85)
        /* compute particle relaxation time */
        taup = rho_s*diam2*diam2/18./mu_g;

    void_g = C_VOF(cell, thread_g); /* gas vol frac*/

    /*compute drag and return drag coeff, k_g_s*/
    afac = pow(void_g, 4.14);
    if(void_g<=0.85)
```

83
bfac = 0.26*pow(void_g, 1.28);
else
    bfac = pow(void_g, 9.56872);

vfac = 0.5*(afac-0.06*reyp+sqrt(0.0036*reyp*reyp+0.12*reyp*(2.*bfac-
    afac)+afac*afac));

fdrgs =
    void_g*((24/reyp)*(1+0.8943*pow(reyp, 0.3952))+(4.3215/(1+(160.1567/reyp))))/
    (24.0*pow(vfac, 2));

k_g_s = (1.-void_g)*rho_s*fdrgs/taup;

return k_g_s;
Table 11: MFIX DAT File Example

# Fluidized Bed Simulation
# Mario A. Ruvalcaba 11-05-12
# Run time for F90 allocatable arrays on Octane -- 3.3 h
# Run-control section
# RUN_NAME = 'Fluidized-Bed'
DESCRIPTION = 'Fluidized Bed Simulation'
RUN_TYPE = 'new'
UNITS = 'cgs'
TIME  = 0.0  TSTOP = 1.0  DT = 1.0E-3  DT_MIN = 1.0E-12
NORM_G = 0.0d0  NORM_S = 0.0d0  MAX_NIT = 30
DISCRETIZE = 9*2
ENERGY_EQ = .FALSE.
SPECIES_EQ = .FALSE.  .FALSE.
#
# Physical Parameters
# UR_FAC(1) = 0.5
!
! Geometry Section
!
COORDINATES = 'cartesian'
XLENGTH = 12.0 !X length
IMAX = 160 !cells in i direction
YLENGTH = 50.0 !height
JMAX = 220 !cells in j direction
NO_K = .TRUE. !2D, no k direction

GRAVITY = 980
#
# Gas-phase Section
#
MU_g0 = 1.8E-4
MW_avg = 29.
#
# Solids-phase Section
#
DRAG_TYPE = 'SYAM_OBRIEN'
DRAG_c1 = 0.26
DRAG_d1 = 9.56872
RO_s = 2.23
D_p0 = 0.1
e = 0.8
Phi = 0.0
EP_star = 0.35
# # Initial Conditions Section #
#
#               Bed       Freeboard
# IC_X_w           =  0.0             0.0
# IC_X_e           =  12.0            12.0
# IC_Y_s           =  0.0             5.5
# IC_Y_n           =  5.5            50.0
# IC_EP_g          =  0.35            1.0
# IC_U_g           =  0.0             0.0
# IC_V_g           = @(45.8/0.45)      45.8
# IC_U_s(1,1)      =  0.0             0.0
# IC_V_s(1,1)      =  0.0             0.0
# IC_P_star        =  0.0             0.0
# IC_T_g           = 300.0          300.0
#
# # Boundary Conditions Section #
#
#               Inlet       Outlet
# BC_X_w           =     0.0      0.0
# BC_X_e           =     12.0     12.0
# BC_Y_s           =     0.0     50.0
# BC_Y_n           =     0.0     50.0
# BC_TYPE          =    'MI'     'PO'
# BC_EP_g          =    1.0
# BC_U_g           =    0.0
# BC_V_g           =  1.000.0
# BC_P_g           = 1.013E6   1.013E6
# BC_T_g           = 300.0
#
# # Output Control #
#
# RES_DT = 0.01
# ! EP_g P_g       U_g  U_s  ROP_s     T_g  X_g
# ! P_star V_g V_s T_s1 X_s     Theta Scalar
# ! W_g W_s T_s2
# SPX_DT = 0.01 0.1 0.1 0.1 100.     100. 100. 100.0 100.0

NLOG   = 100
full_log = .true.
Table 12: Experimental Drag Coefficient and Reynolds Number Data

<table>
<thead>
<tr>
<th>Re</th>
<th>C_{D-exp}</th>
<th>C_{D-cal}</th>
<th>(\log(C_{D-exp}) - \log(C_{D-cal}))^2</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.010</td>
<td>2700</td>
<td>2747.77</td>
<td>5.80E-05</td>
</tr>
<tr>
<td>0.011</td>
<td>2550</td>
<td>2510.11</td>
<td>4.69E-05</td>
</tr>
<tr>
<td>0.013</td>
<td>2200</td>
<td>2142.90</td>
<td>1.30E-04</td>
</tr>
<tr>
<td>0.020</td>
<td>1490</td>
<td>1428.68</td>
<td>3.37E-04</td>
</tr>
<tr>
<td>0.025</td>
<td>1323</td>
<td>1159.81</td>
<td>3.27E-03</td>
</tr>
<tr>
<td>0.028</td>
<td>1140</td>
<td>1043.72</td>
<td>1.47E-03</td>
</tr>
<tr>
<td>0.030</td>
<td>934</td>
<td>978.95</td>
<td>4.17E-04</td>
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<td>874</td>
<td>848.74</td>
<td>1.62E-04</td>
</tr>
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<td>0.035</td>
<td>865</td>
<td>848.74</td>
<td>6.80E-05</td>
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<td>850</td>
<td>786.69</td>
<td>1.13E-03</td>
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<td>625</td>
<td>611.39</td>
<td>9.14E-05</td>
</tr>
<tr>
<td>0.050</td>
<td>602</td>
<td>611.39</td>
<td>4.52E-05</td>
</tr>
<tr>
<td>0.060</td>
<td>586</td>
<td>517.67</td>
<td>2.90E-03</td>
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<td>0.065</td>
<td>450</td>
<td>481.34</td>
<td>8.55E-04</td>
</tr>
<tr>
<td>0.075</td>
<td>500</td>
<td>422.82</td>
<td>5.30E-03</td>
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<td>355</td>
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<td>1.33E-03</td>
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<td>335</td>
<td>277.38</td>
<td>6.72E-03</td>
</tr>
<tr>
<td>0.150</td>
<td>250</td>
<td>227.61</td>
<td>1.66E-03</td>
</tr>
<tr>
<td>0.220</td>
<td>170</td>
<td>162.73</td>
<td>3.61E-04</td>
</tr>
<tr>
<td>0.300</td>
<td>155</td>
<td>124.46</td>
<td>9.08E-03</td>
</tr>
<tr>
<td>0.400</td>
<td>105</td>
<td>97.37</td>
<td>1.07E-03</td>
</tr>
<tr>
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<td>90</td>
<td>80.65</td>
<td>2.27E-03</td>
</tr>
<tr>
<td>0.500</td>
<td>90</td>
<td>80.65</td>
<td>2.27E-03</td>
</tr>
<tr>
<td>0.630</td>
<td>74</td>
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<td>2.16E-03</td>
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<td>1.64E-04</td>
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<td>0.850</td>
<td>63</td>
<td>51.94</td>
<td>7.03E-03</td>
</tr>
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<td>55</td>
<td>45.49</td>
<td>6.80E-03</td>
</tr>
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<td>35</td>
<td>39.25</td>
<td>2.48E-03</td>
</tr>
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<td>7.69E-04</td>
</tr>
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<td>30</td>
<td>31.20</td>
<td>2.88E-04</td>
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Vita

Mario Alberto Ruvalcaba was born on December 19th, 1984 in Juarez, MEXICO. The eldest son of Mario Ruvalcaba and Lilia Andrade, he graduated from COBACH #6 High School in Juarez, MEXICO in Spring 2002 and joined The University of Texas at El Paso (UTEP) to pursue a Bachelor of Science in Mechanical Engineering. After the completion of his Bachelor Degree in Fall 2007 he worked as a CFD engineer at Delphi Automotive Systems, at the same time he began attendance in the same university to pursue a Master Degree in Mechanical Engineering. He started working at the Combustion and Propulsion Research Laboratory under the supervision of Dr. Ahsan Choudhuri, where the facilities few years later became the Center for Space Technology Research where he currently performs.

Mario Alberto Ruvalcaba obtained his Master degree in Mechanical Engineering in Summer 2009. Eventually he enrolled in the Engineering Doctoral program working towards his PhD in Energy Science and Engineering. Ruvalcaba has been the recipient of various honors and awards including the Artemio de la Vega Memorial Scholarship and the State of Texas Public Education Grant (TPEG) for International Students. While pursuing his degree, Ruvalcaba’s research was focused on the CFD modeling of multiphase flow problems such as gas-solid fluidization technologies. Mario Alberto Ruvalcaba has presented his research at international conference meetings and workshops including the 2011 Annual International Energy Conversion Engineering Conference in San Diego, CA.

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This dissertation was typed by Mario Alberto Ruvalcaba